



# The biological motor

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Syn Schmitt

Department of Sports and Exercise Science, University of Stuttgart  
The Human Movement Simulation Lab, Allmandring 28

Stuttgart Research Centre for Simulation Technology, University of Stuttgart  
Pfaffenwaldring 5a



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*The Human Movement  
Simulation Lab*





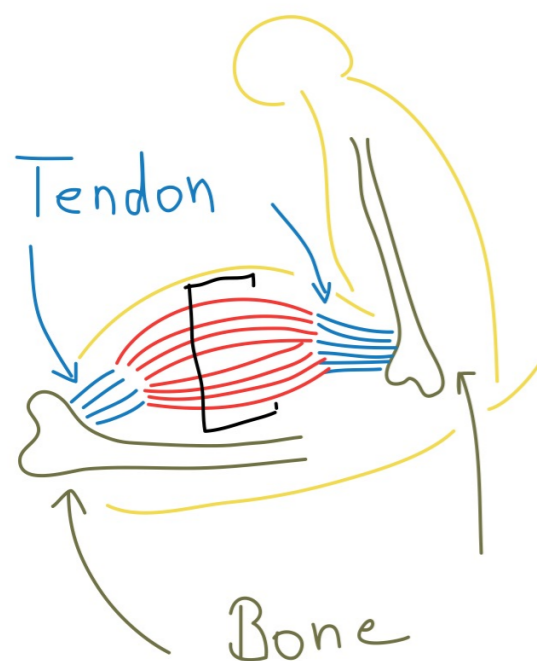
# The biological skeletal muscle's ...

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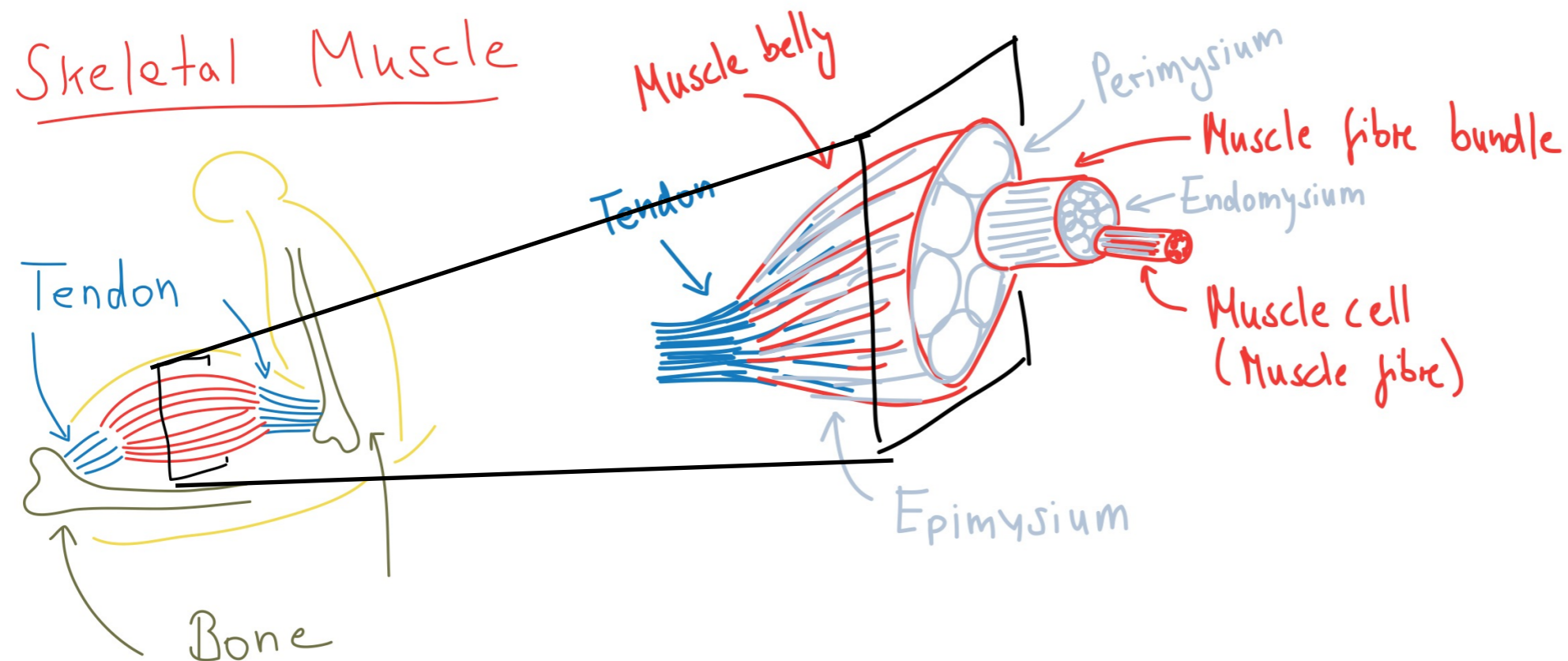
anatomy, physiology, and metabolism.

# Biological skeletal muscle's anatomy

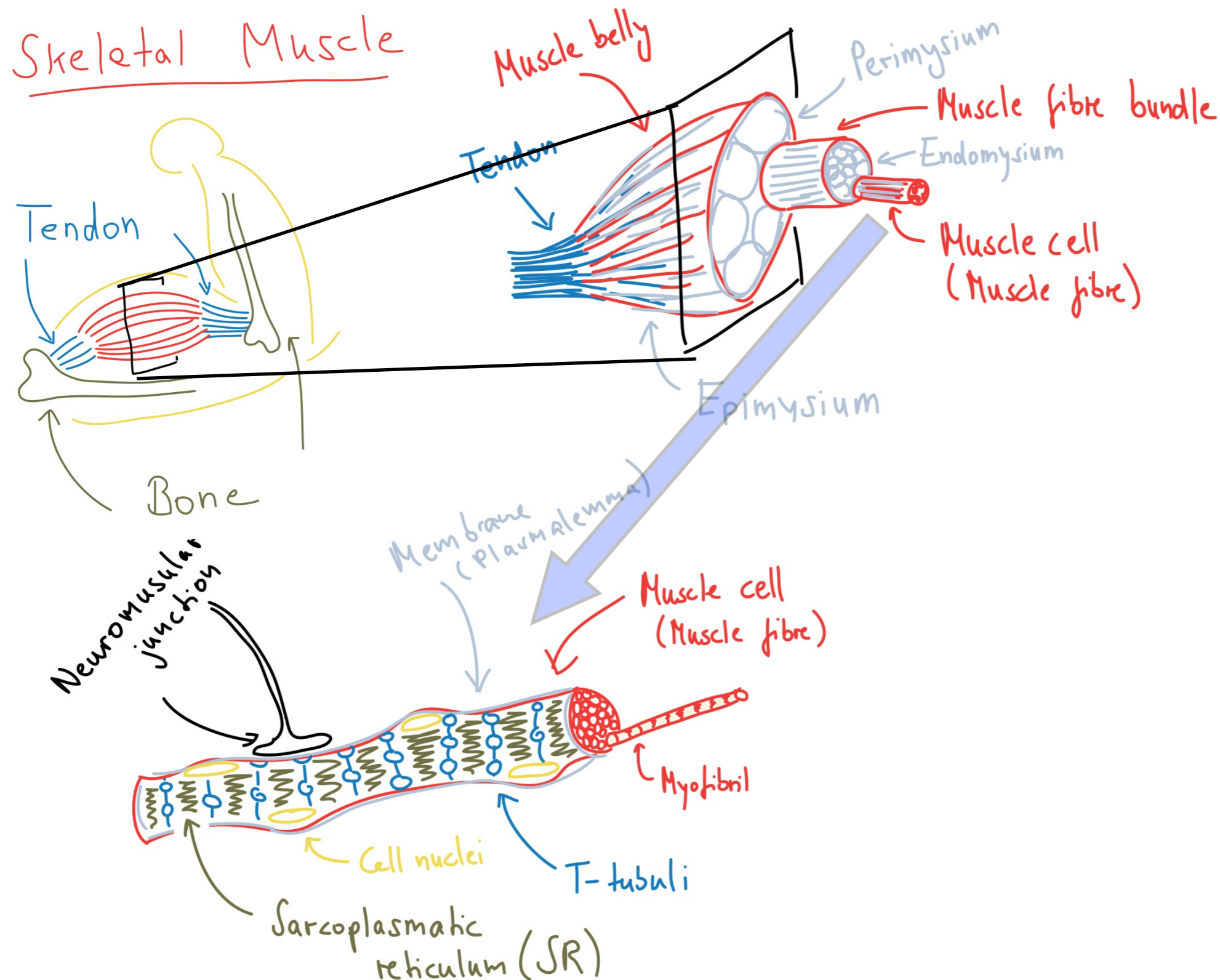
## Skeletal Muscle



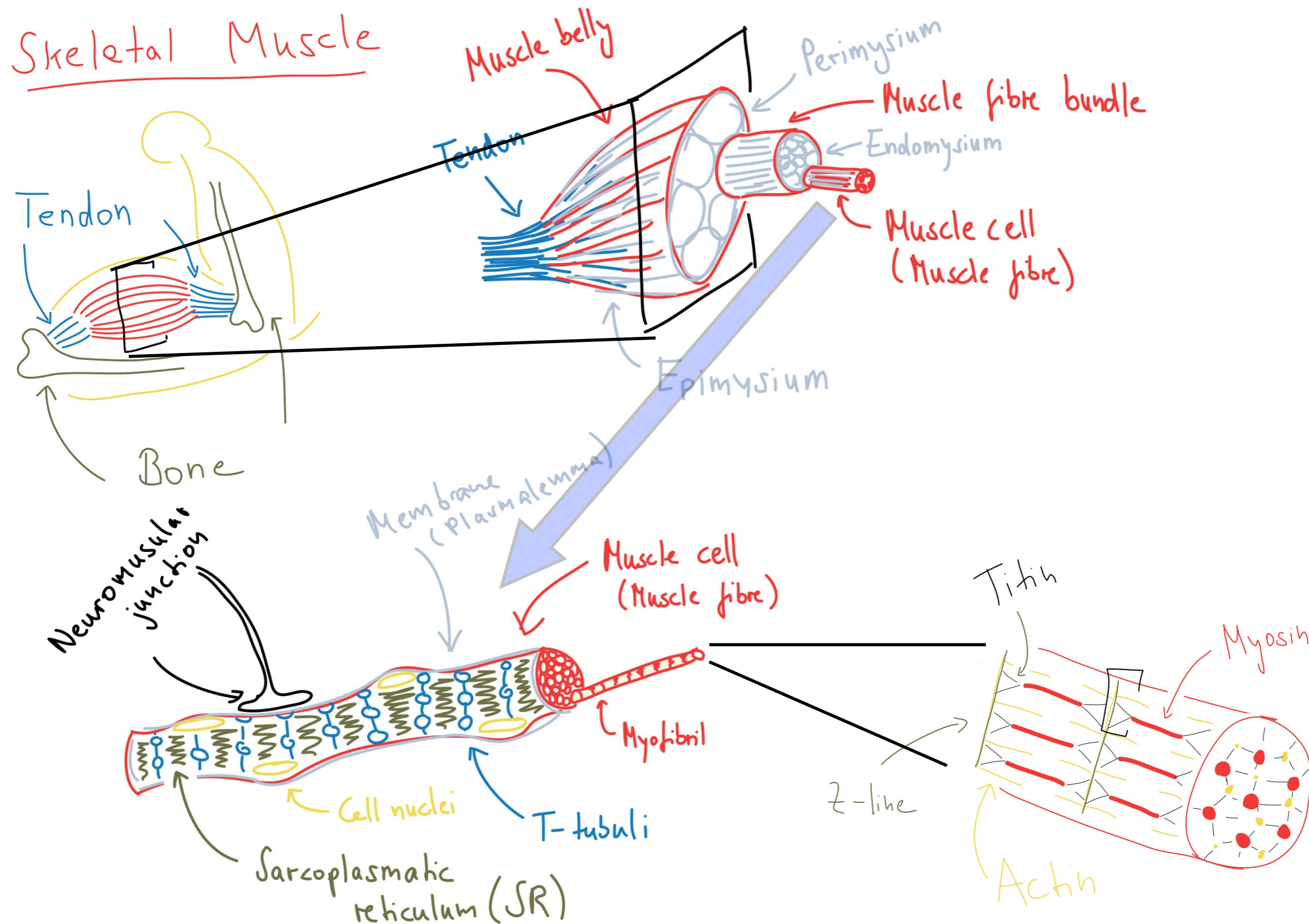
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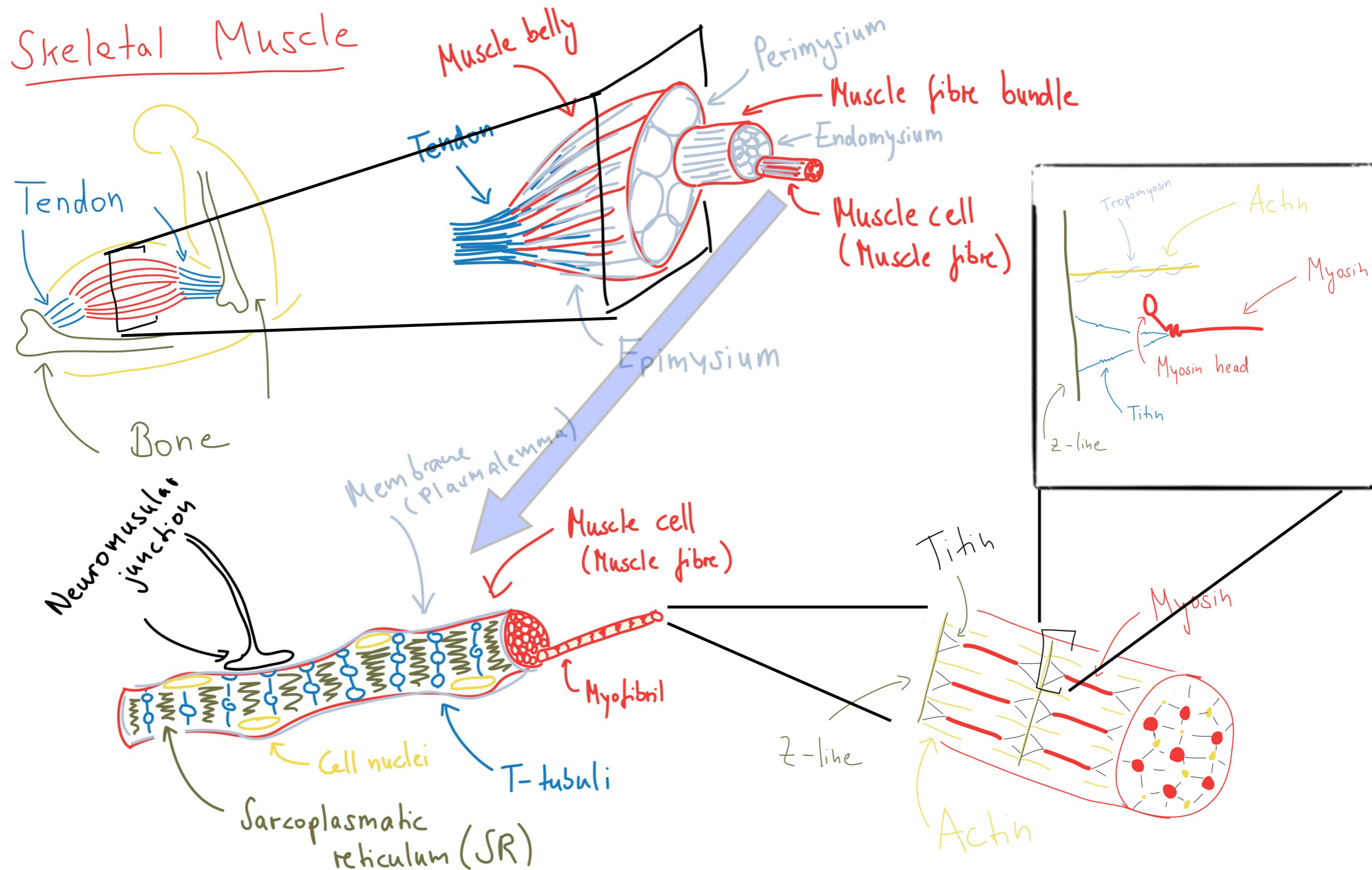
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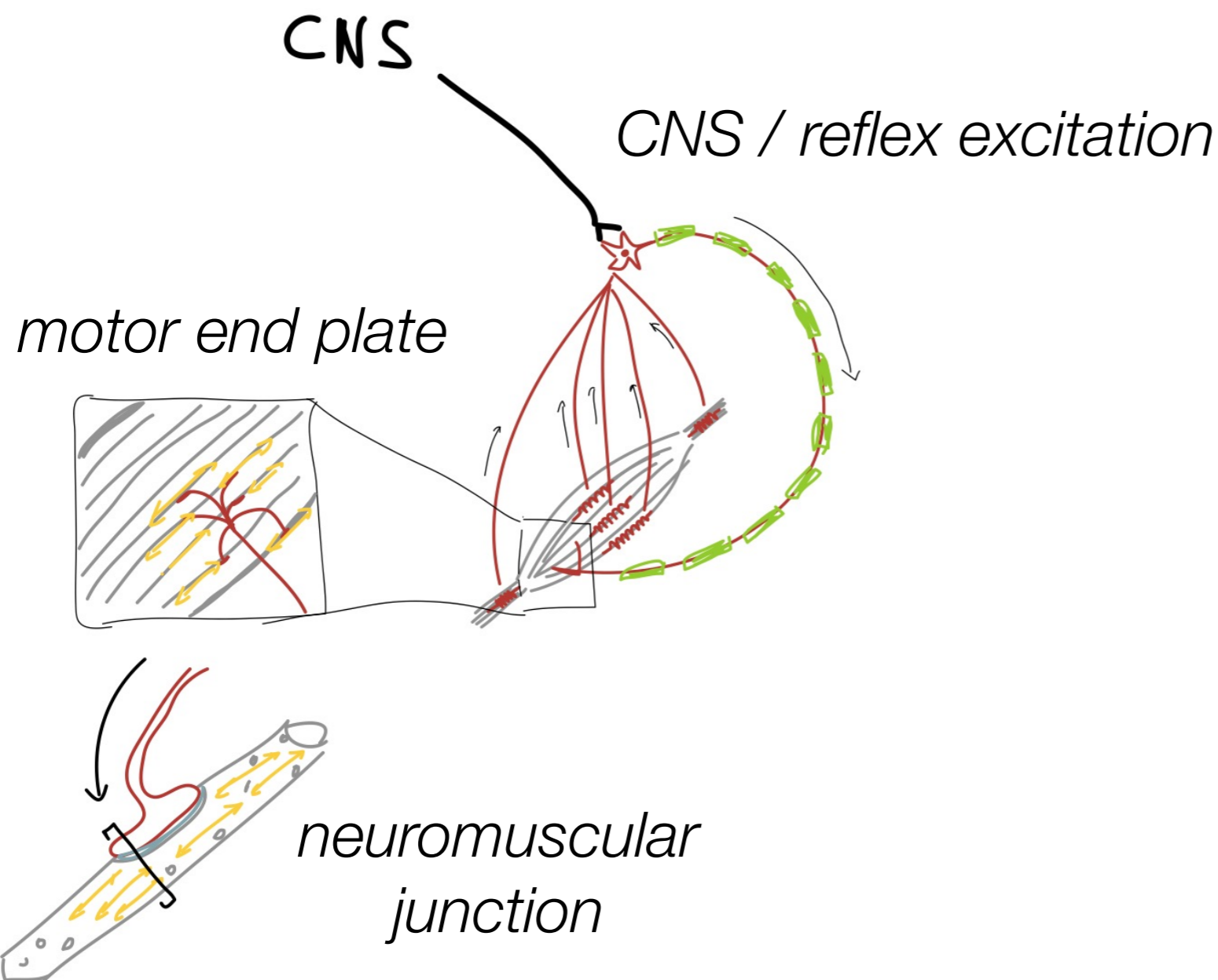
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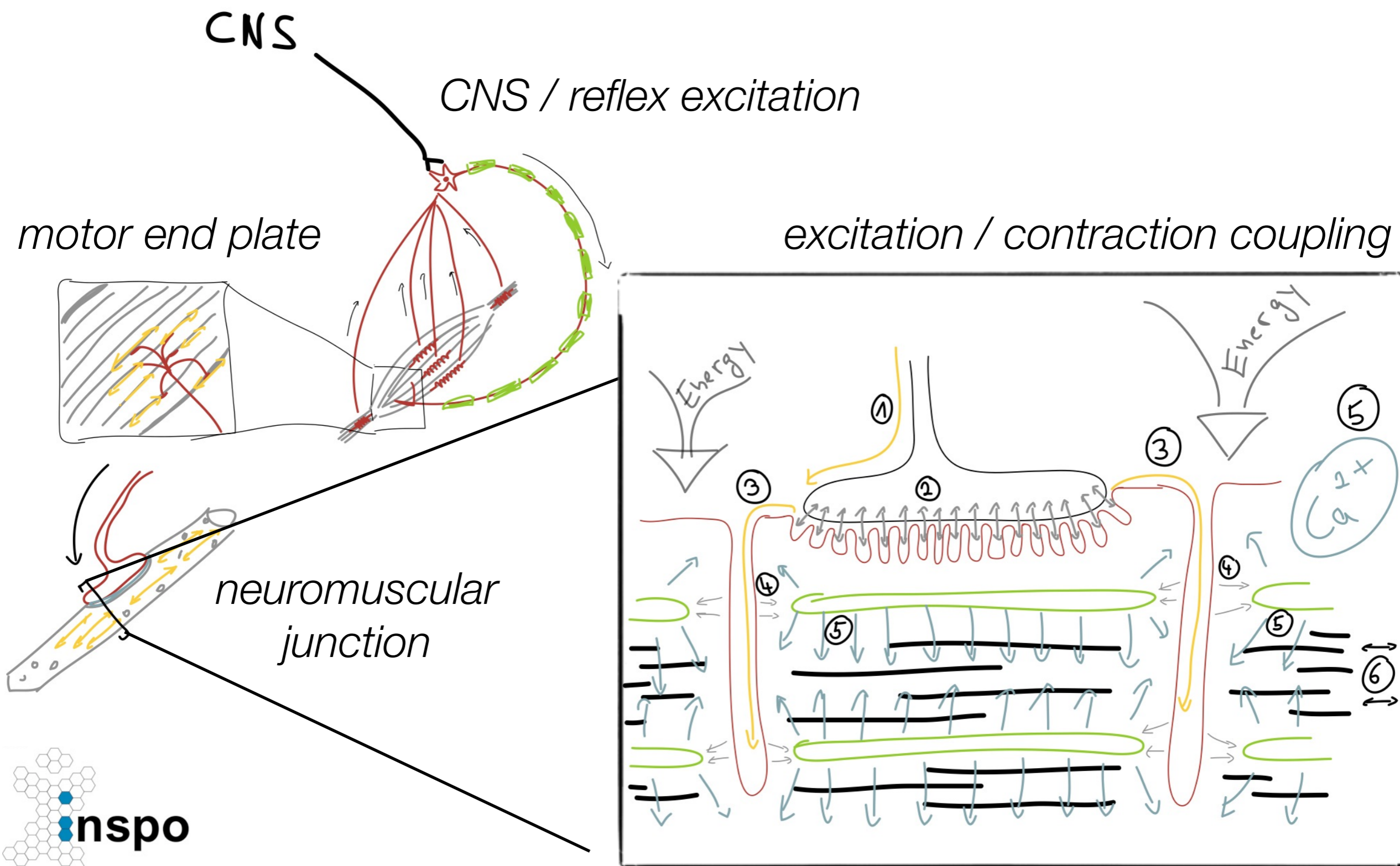
# Biological skeletal muscle's anatomy



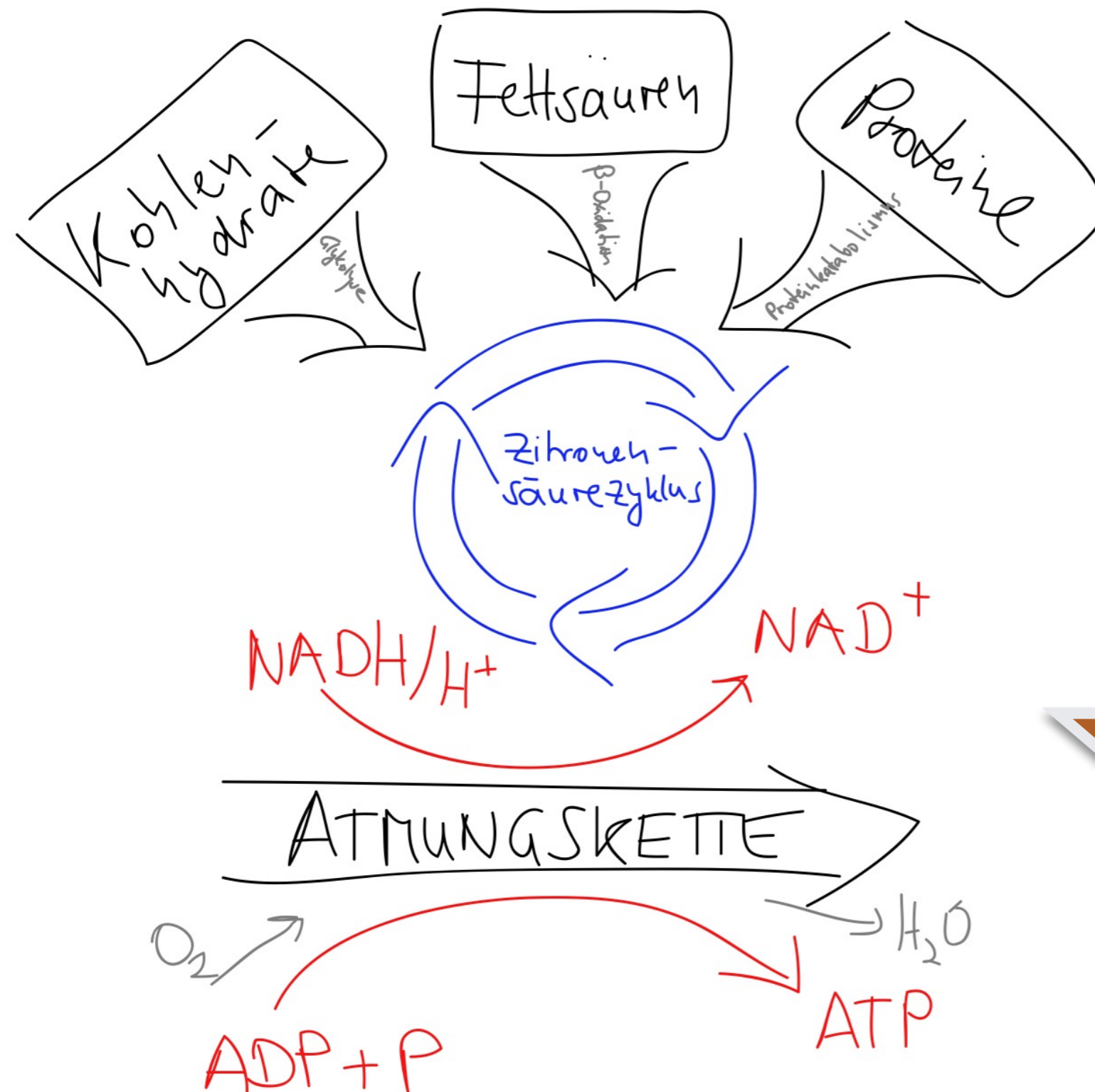
# Biological skeletal muscle's physiology



# Biological skeletal muscle's physiology



# Biological skeletal muscle's metabolism



Fuel / energy supply

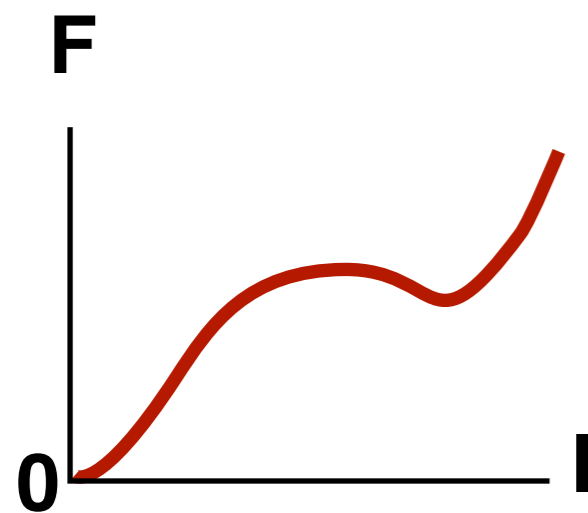


# The biological skeletal muscle's ...

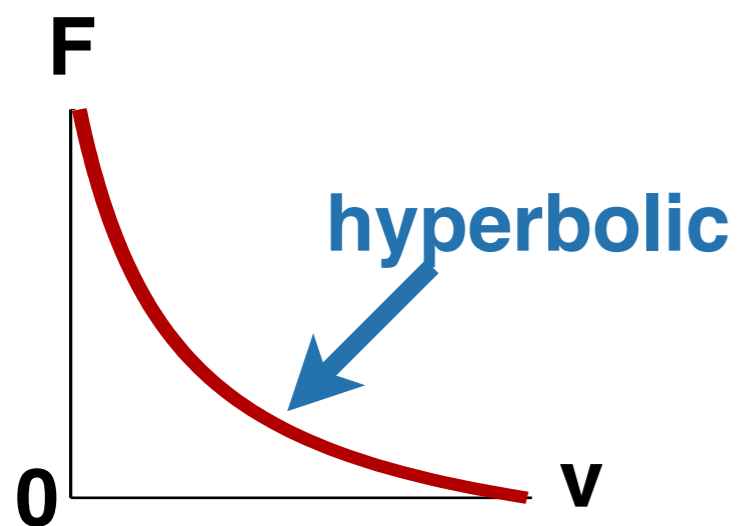
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mechanics and thermodynamics.

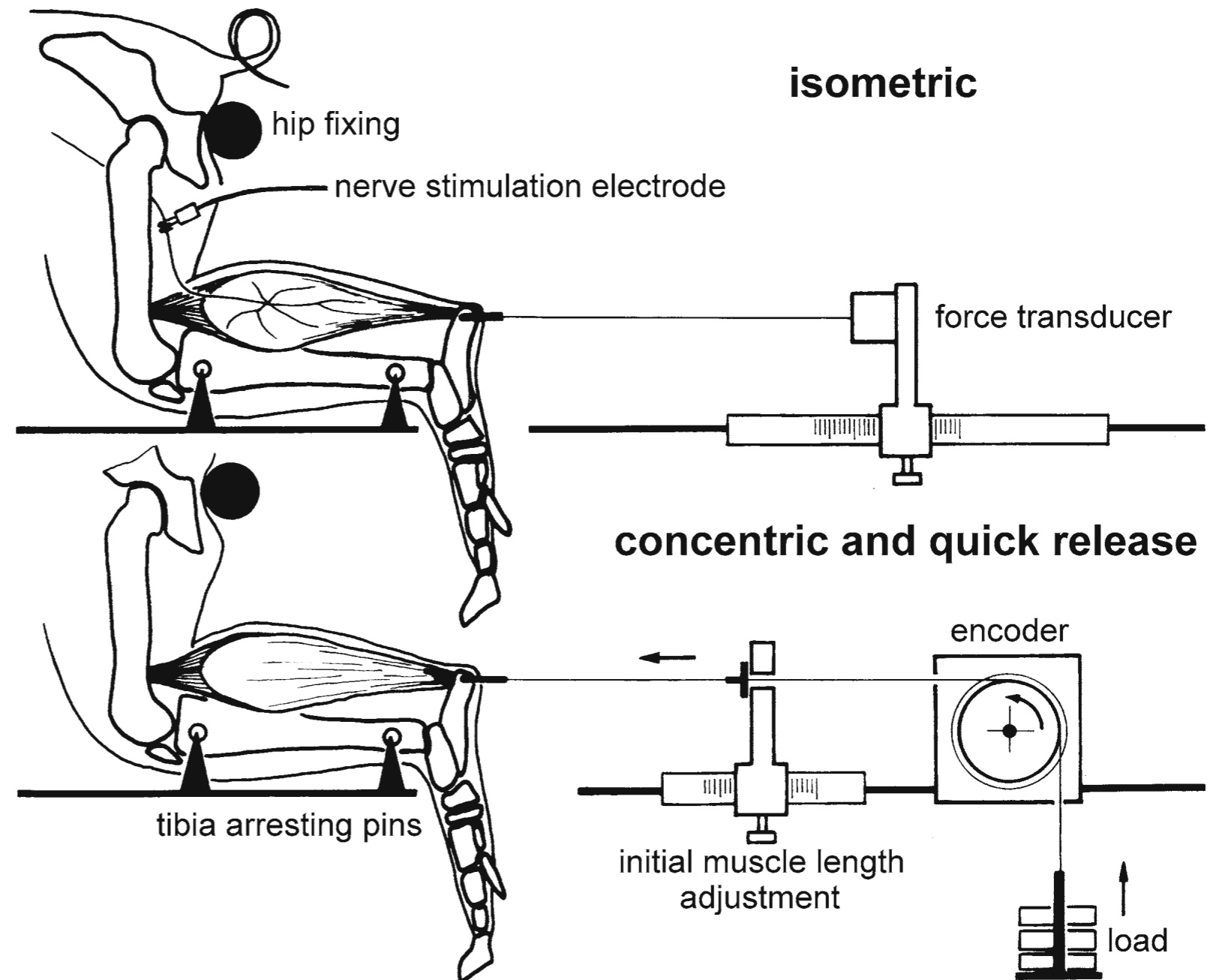
# Skeletal muscle's mechanical characteristics



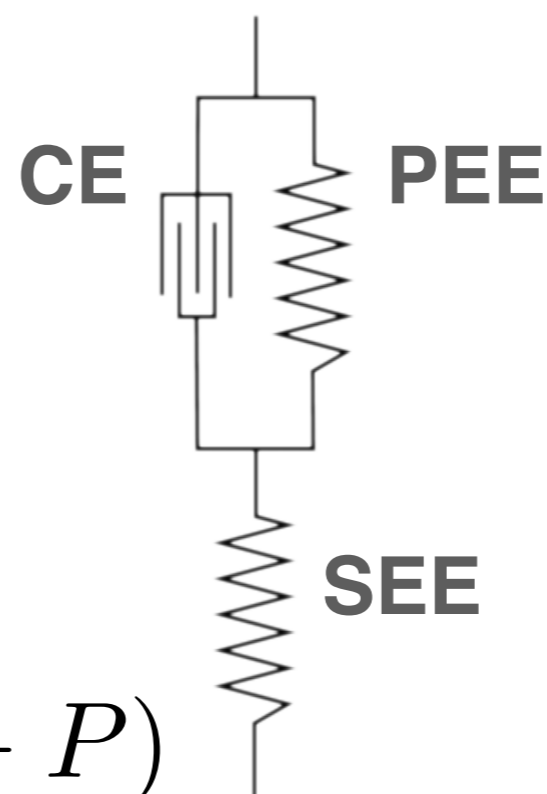
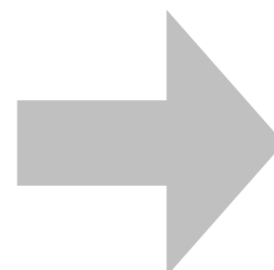
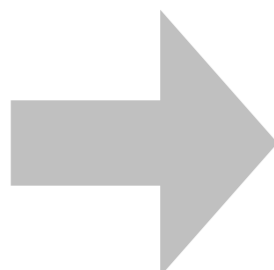
**Force-length  
relationship**



**Force-velocity  
relation**



# Skeletal muscle's mechanical characteristics



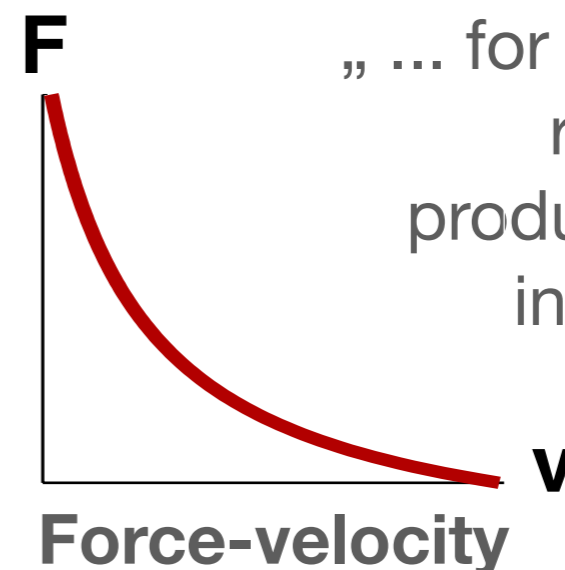
$$(P + a) \cdot v = b \cdot (P_0 - P)$$



Archibald Vivian Hill

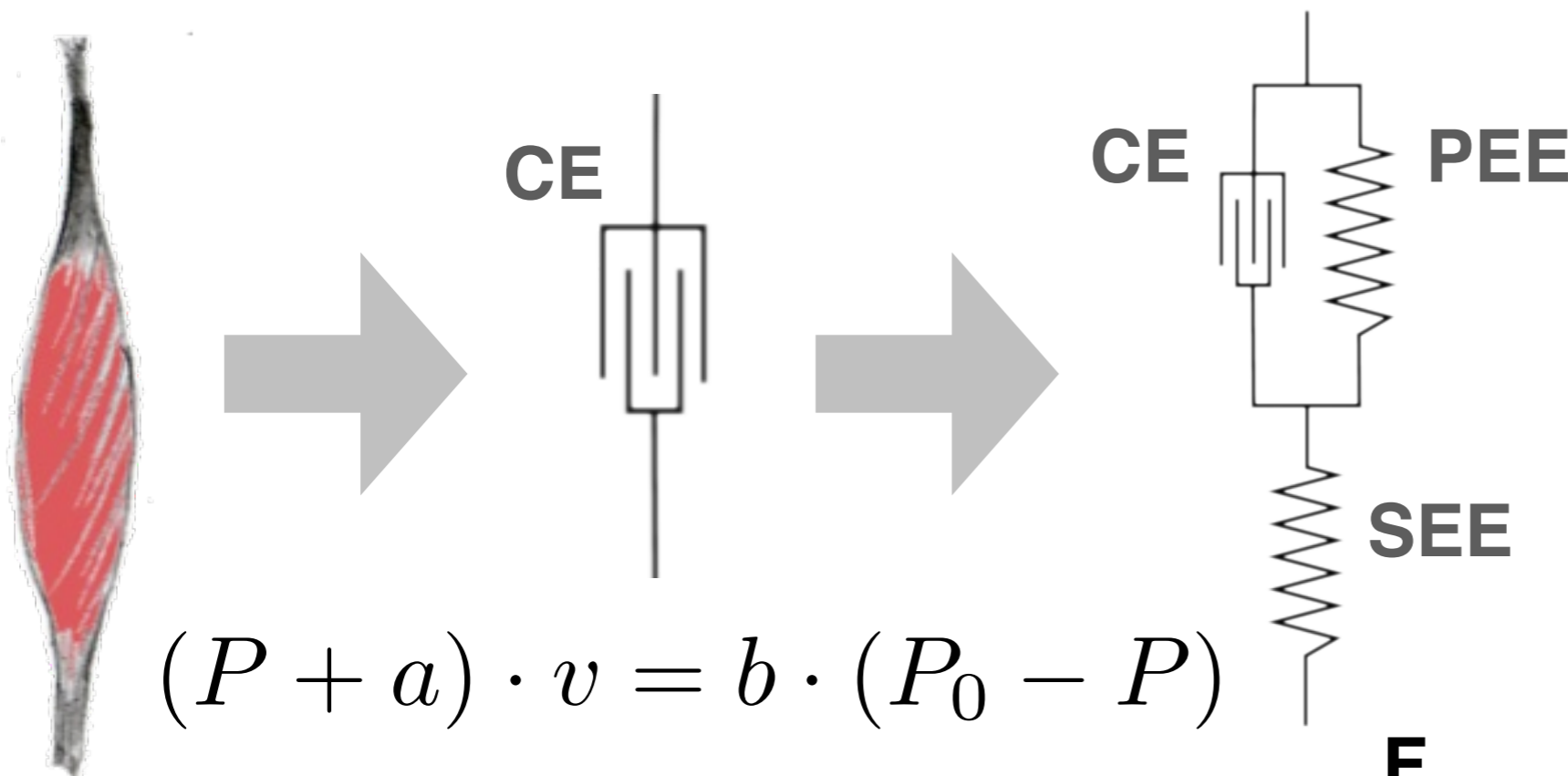
**Nobel Prize 1922:**

„ ... for his discovery relating to the production of heat in the muscle.“



Hill, A., 1938. The heat of shortening and the dynamic constants of muscle. Proceedings of the Royal Society of London B 126, 136–195.

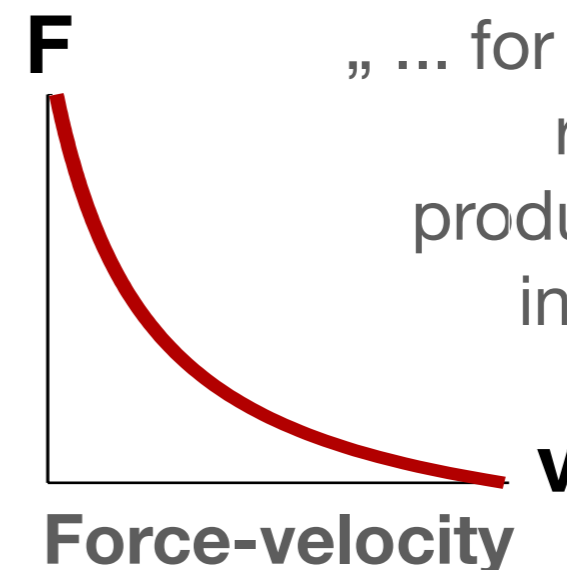
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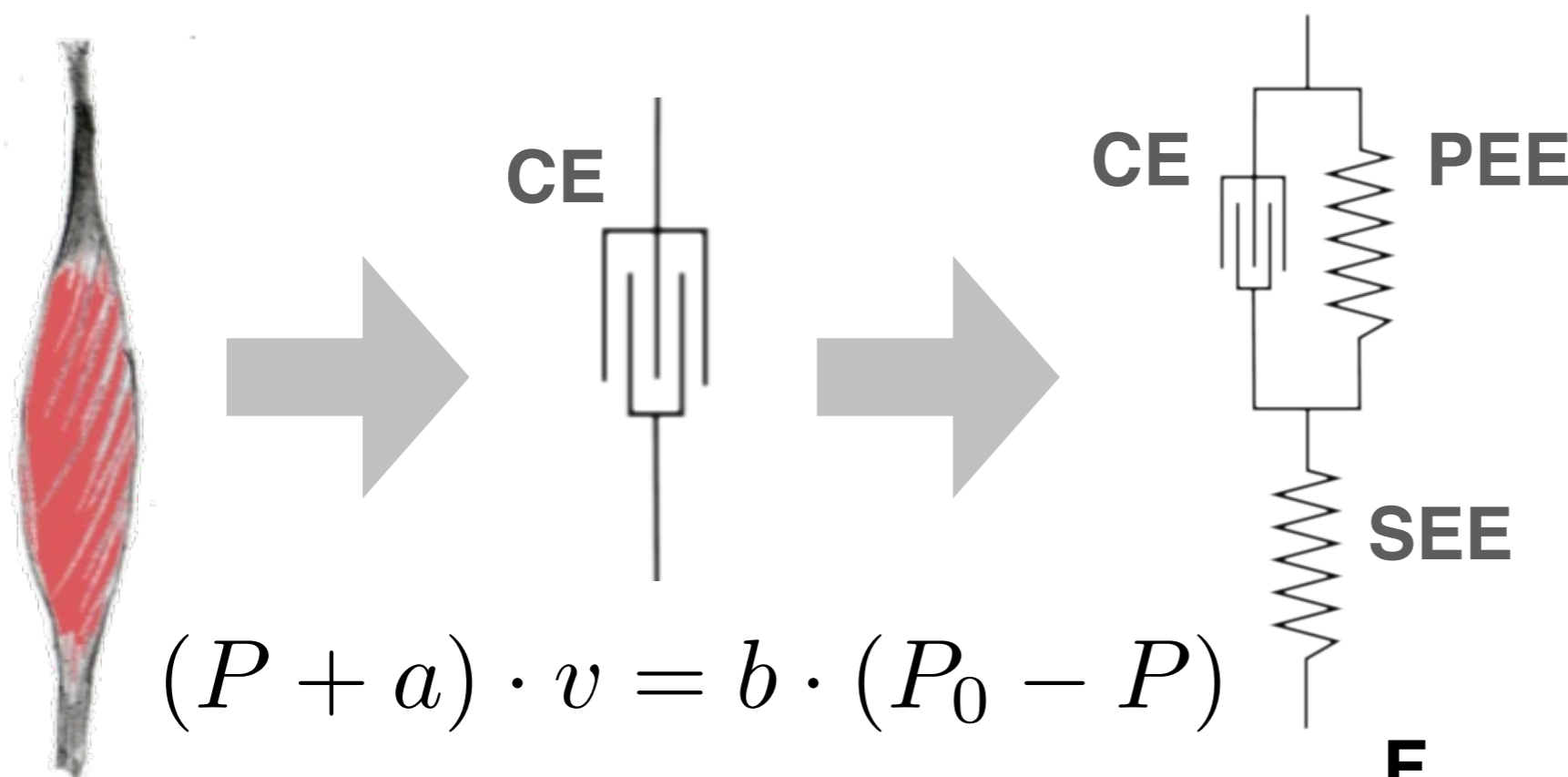
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Hill-type muscle models include a  
**contractile element** which represents  
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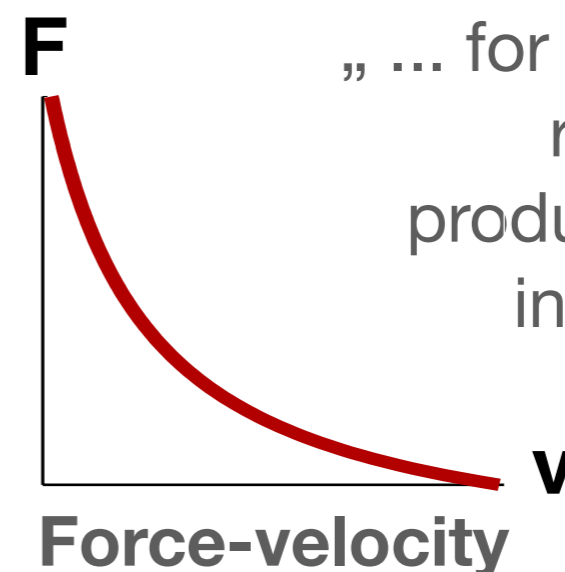


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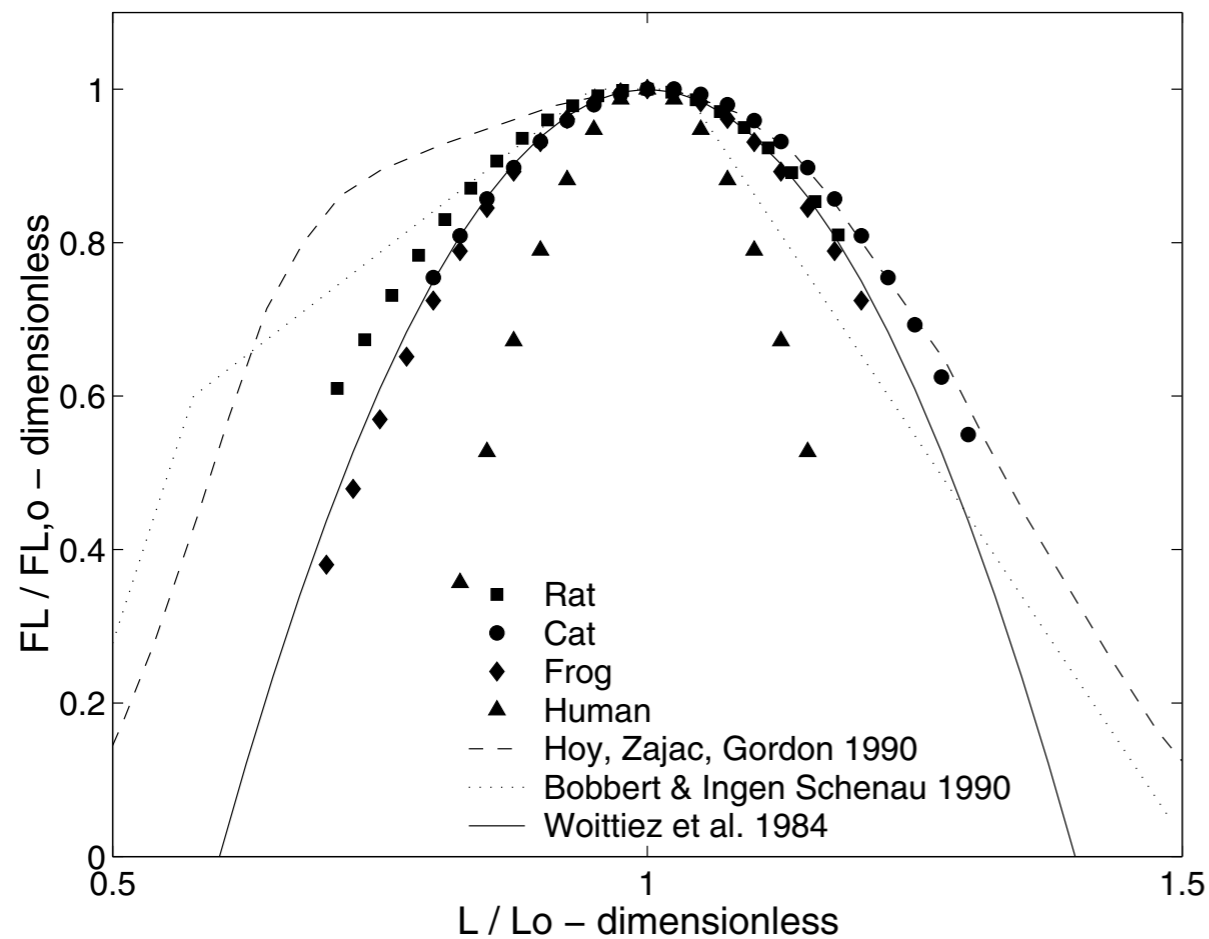


Hill-type muscle models include a **contractile element** which represents the **empirical force-velocity data**

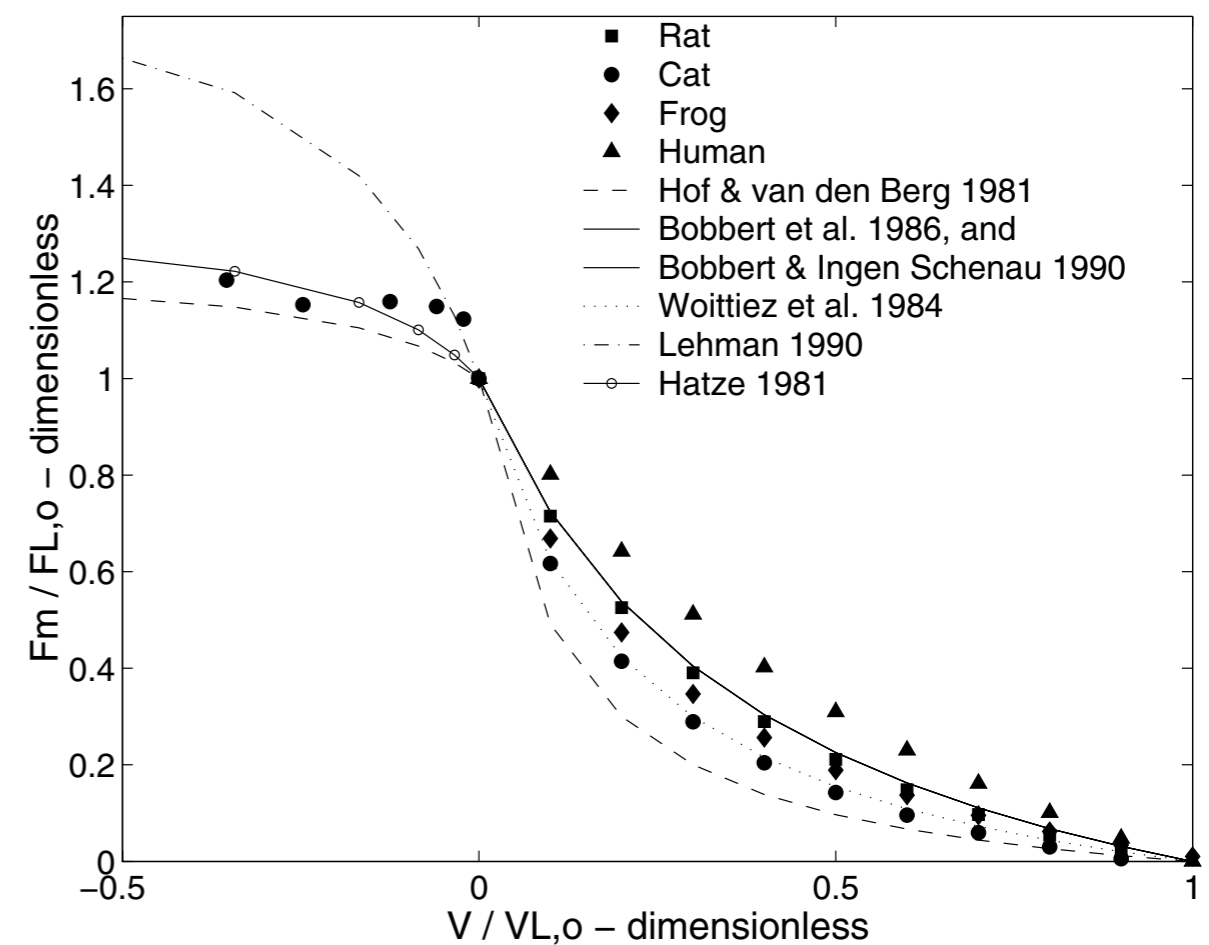


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# Skeletal muscle's mechanical characteristics

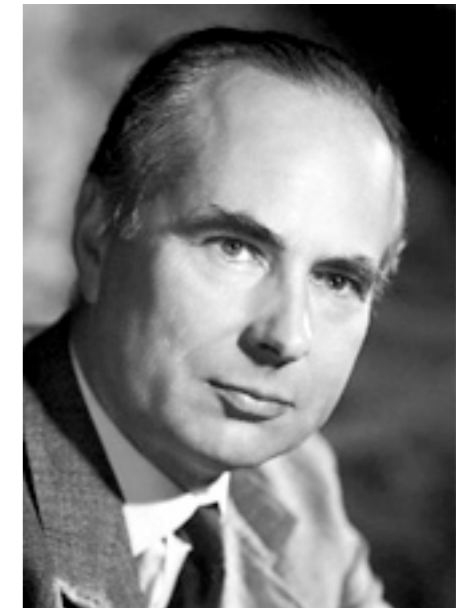
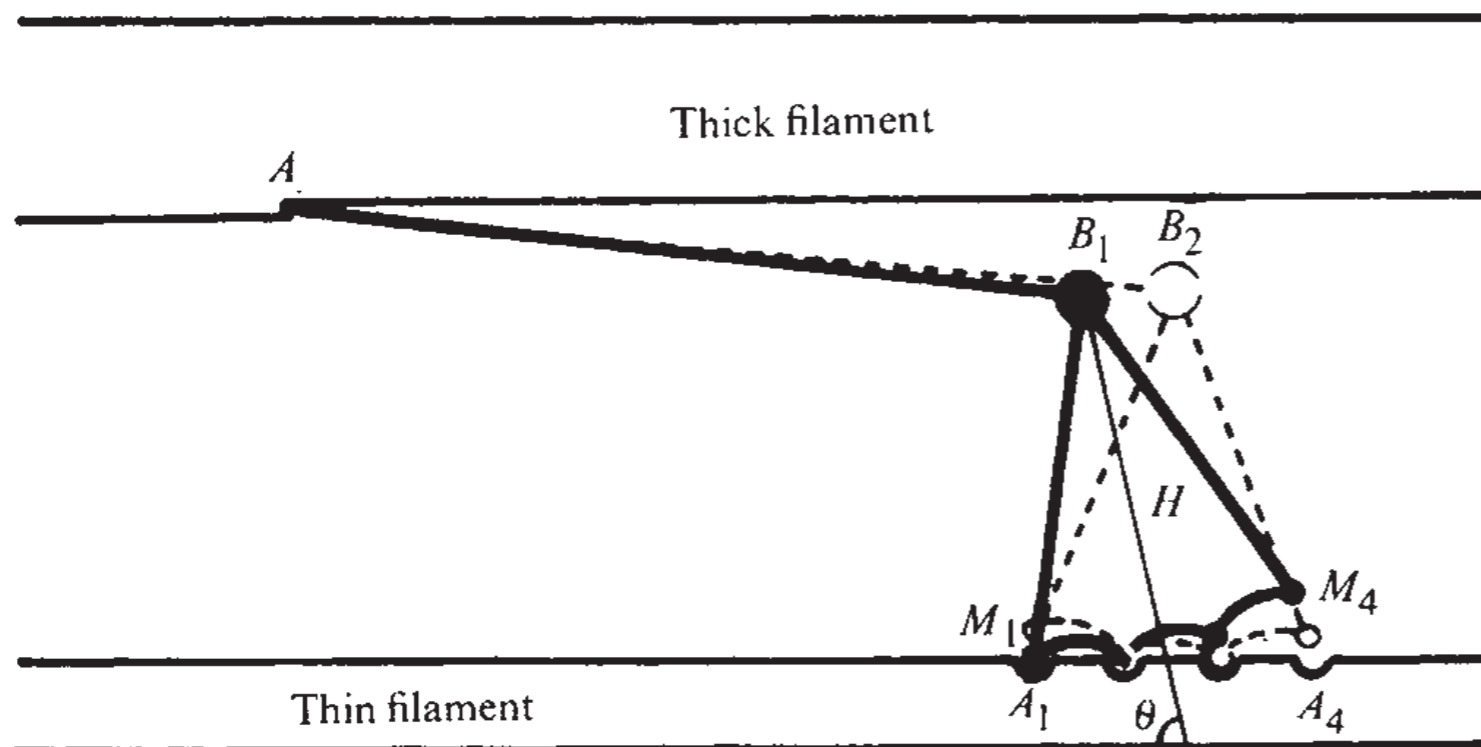


	$k_1$	$k_2$	$k_3$	$L_o$	$F_{L,o}$	
Rat <sup>1</sup>	-4.50	8.95	-3.45	27.0 mm	0.29 N	$p \leq 0.001$
Frog <sup>2</sup>	-6.79	14.69	-6.88	31.0 mm	0.67 N	$r^2 = 0.96$
Cat <sup>3</sup>	-5.71	11.52	-4.81	31.9 mm	0.18 N	$r^2 = 0.99$
Human <sup>4</sup>	-13.43	28.23	-13.96	215.9 mm	193.1 N	$r^2 = 0.75$
Skeletal Muscle Model <sup>5</sup>	-6.25	12.50	-5.25	60.0 mm	3000 N	—



	$a / F_{L,o}$ dimensionless	$F_{L,o}$ N	$b / V_{L,o}$ dimensionless	$V_{L,o}$ mm/s
Rat <sup>1</sup>	0.356	4.30	0.38	144
Frog <sup>2</sup>	0.27	0.67	0.28	42
Cat <sup>3</sup>	0.27	0.18	0.30	191
Human <sup>4</sup>	0.81	200	0.81	1115
Skeletal Muscle Model <sup>5</sup>	0.224	—	0.224	—
Human <sup>6</sup>	0.41	3000	0.39	756
Human <sup>7</sup>	0.41	2430	0.41	780
Human <sup>8</sup>	0.12	—	0.12	—

# Skeletal muscle's mechanical characteristics



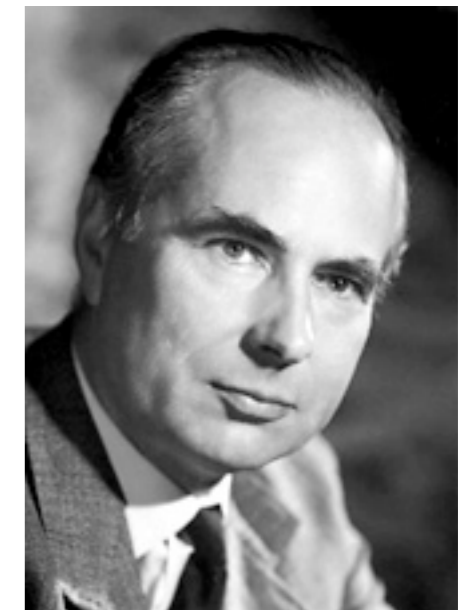
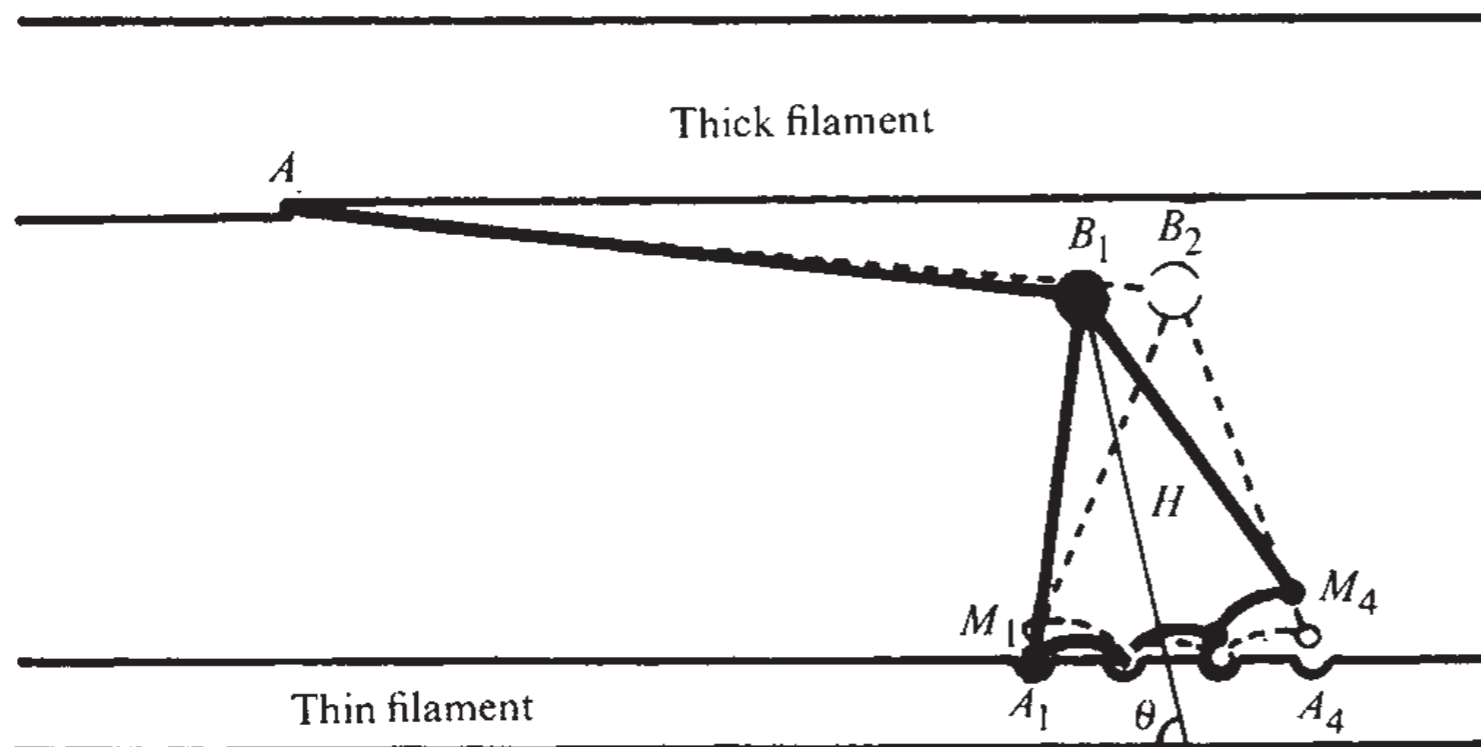
Andrew Fielding Huxley

**Nobel prize 1963:**

„ ... for ... ionic mechanisms involved in excitation ... of the ... cell membrane.“

Huxley, A. F., Niedergerke, R., 1953. Structural changes in muscle during contraction. Interference microscopy of living muscle fibres. *Nature* 173 (4412), 971–973.

# Skeletal muscle's mechanical characteristics



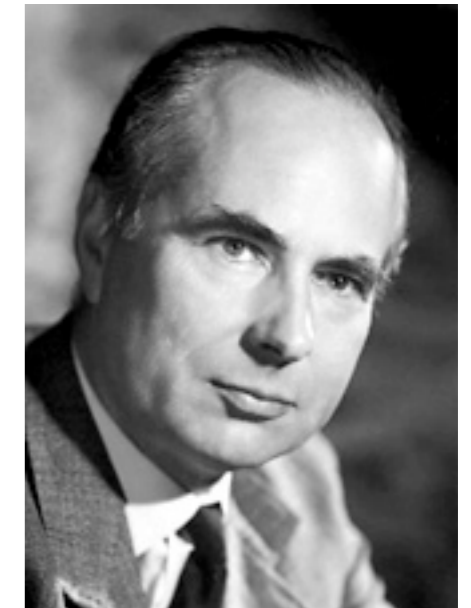
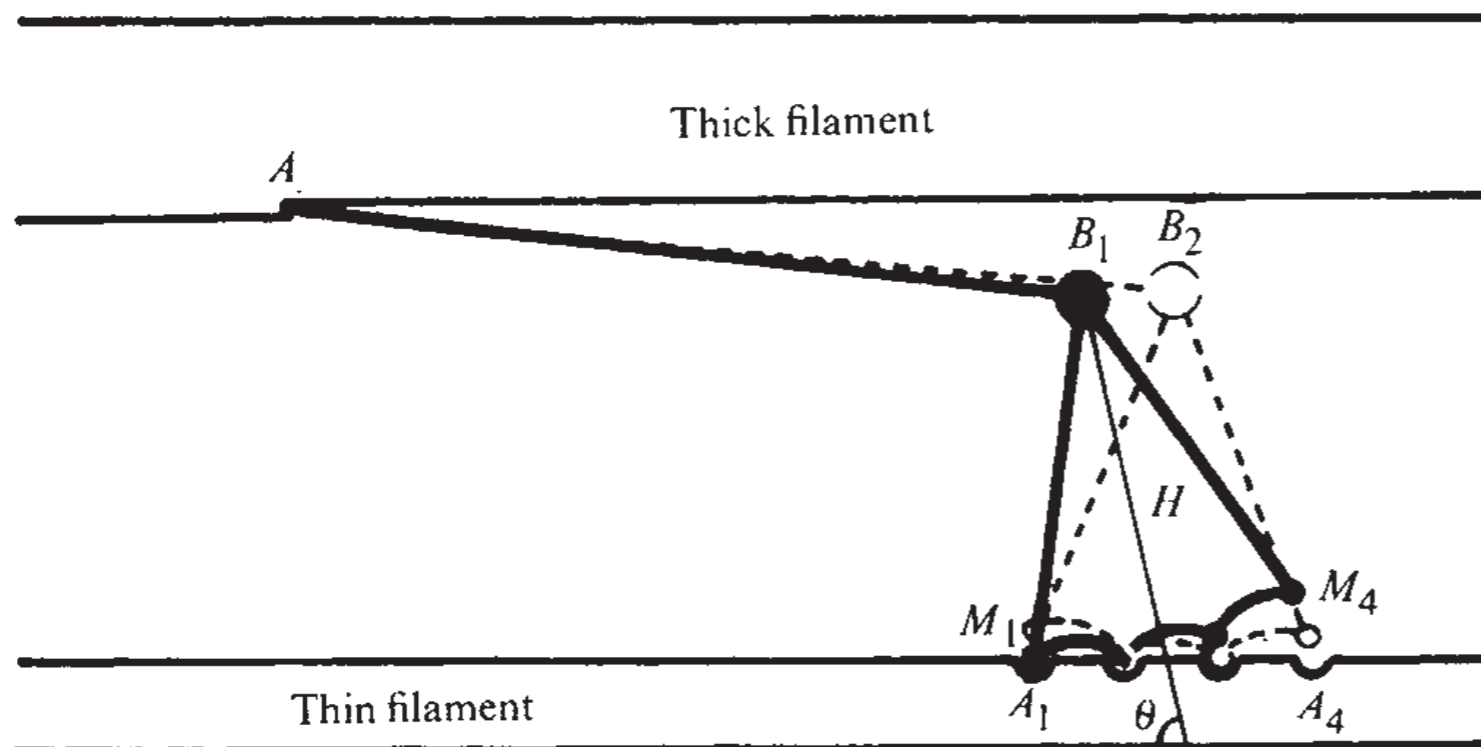
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# Skeletal muscle's mechanical characteristics



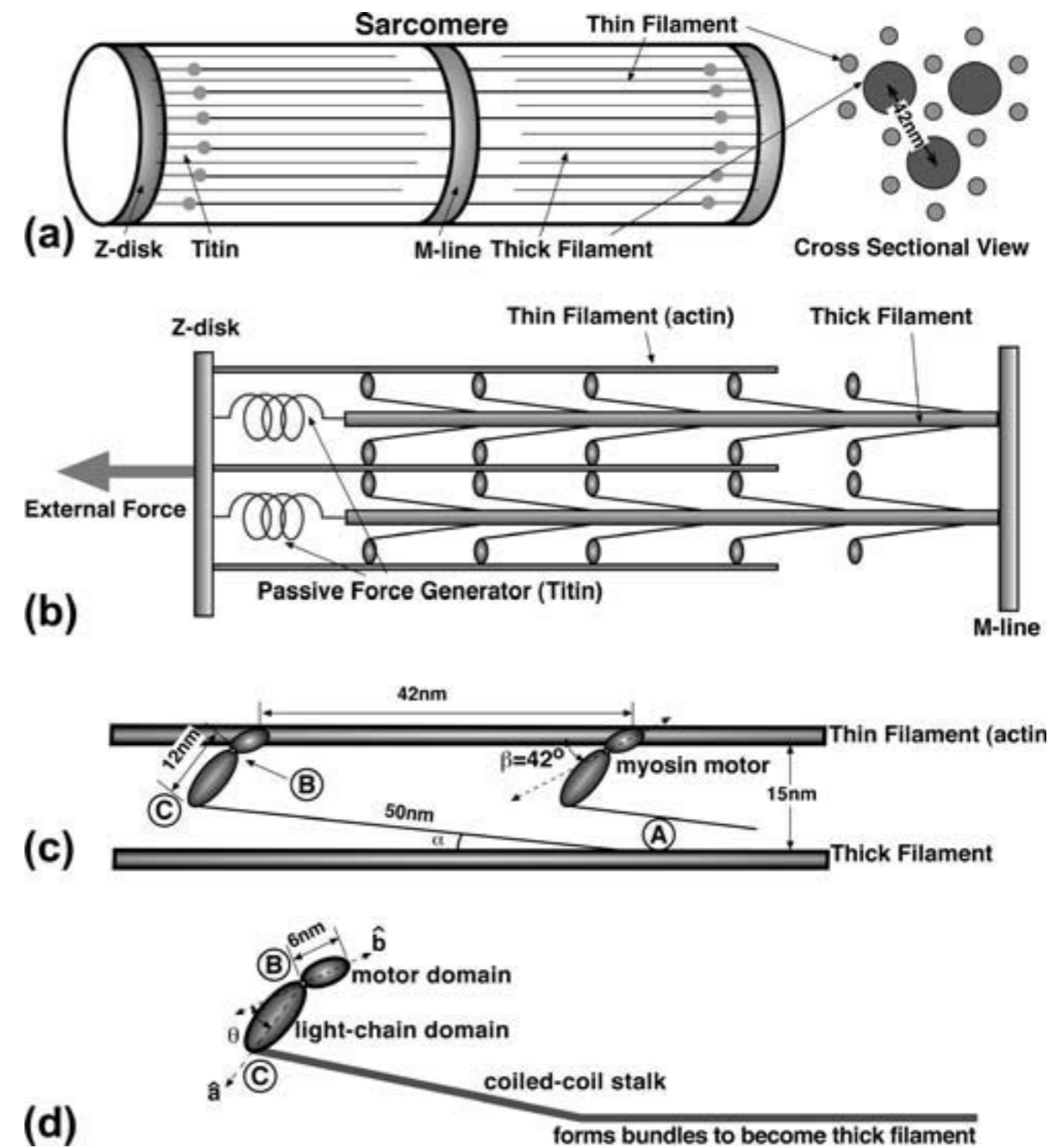
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# Skeletal muscle's mechanical characteristics



Lan, G., Sun, S., 2005. Dynamics of myosin-driven skeletal muscle contraction: I. Steady-state force generation. Biophysical Journal 88 (6), 4107– 4117.

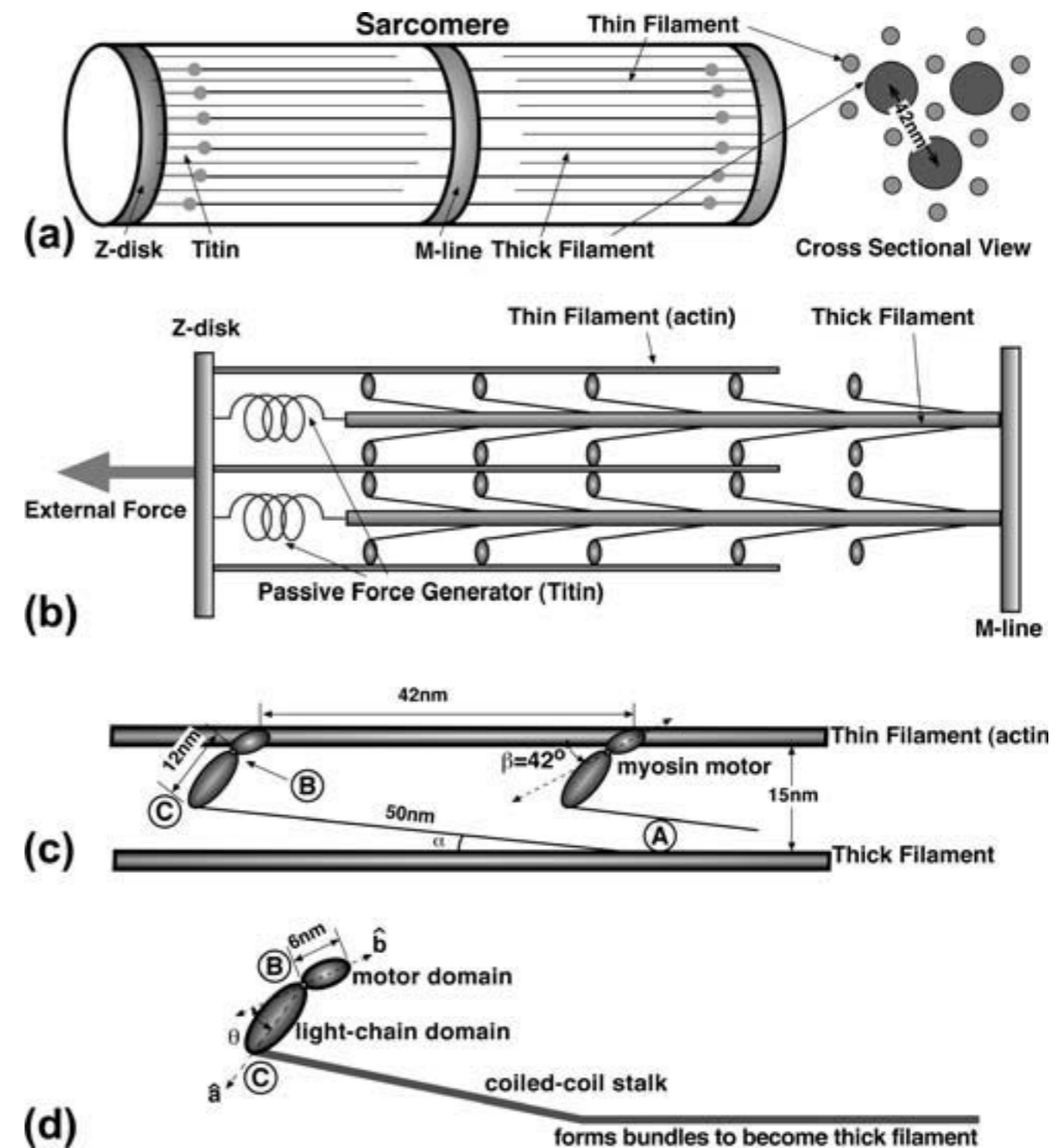
# Skeletal muscle's mechanical characteristics

Huxley-type model describing myosin head movement

Presets force and chemical state

Include molecular friction, chemical kinetics and a stochastic component

Predicts change of muscle coordinate (angle of myosin heads)



Lan, G., Sun, S., 2005. Dynamics of myosin-driven skeletal muscle contraction: I. Steady-state force generation. Biophysical Journal 88 (6), 4107– 4117.

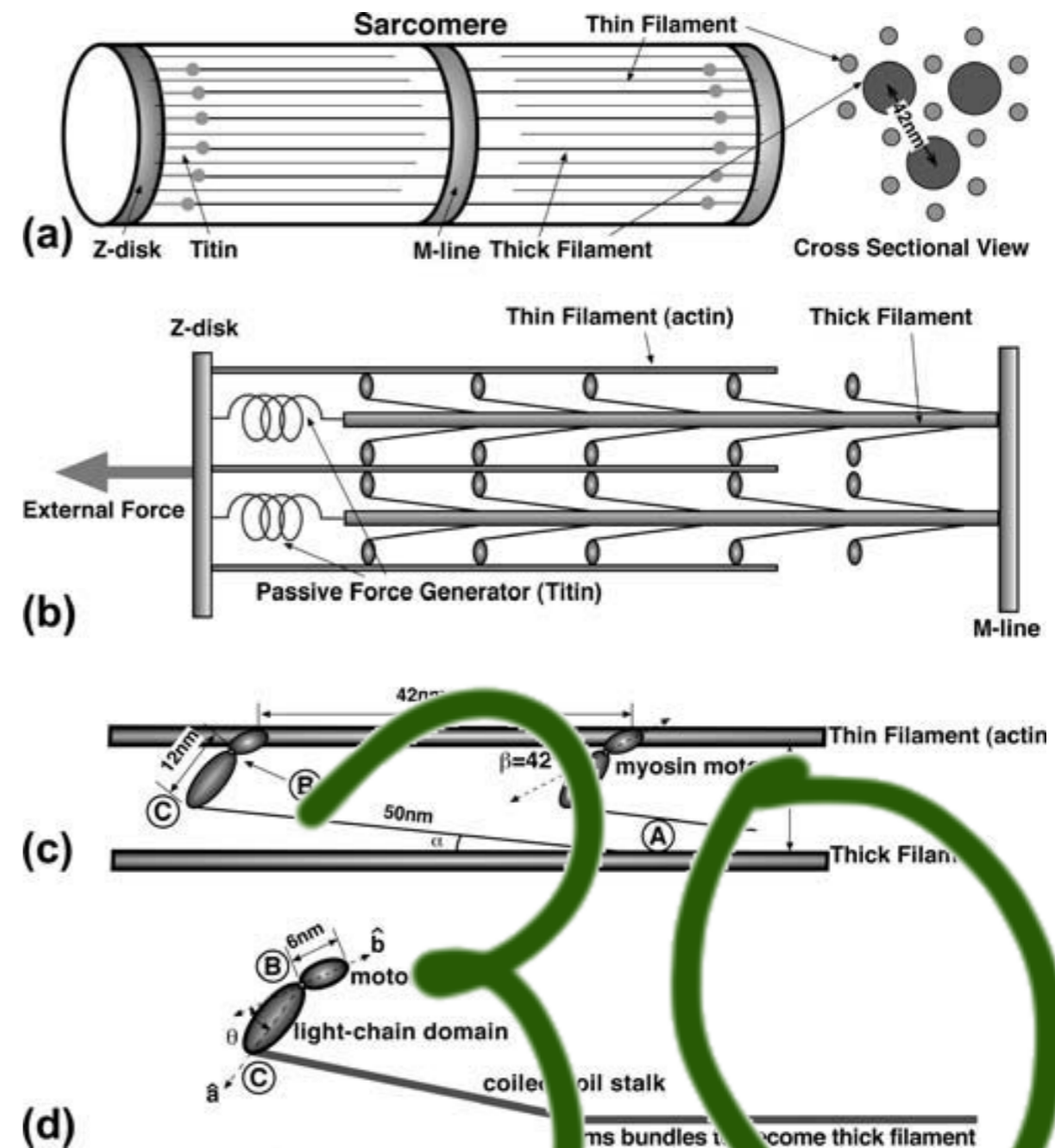
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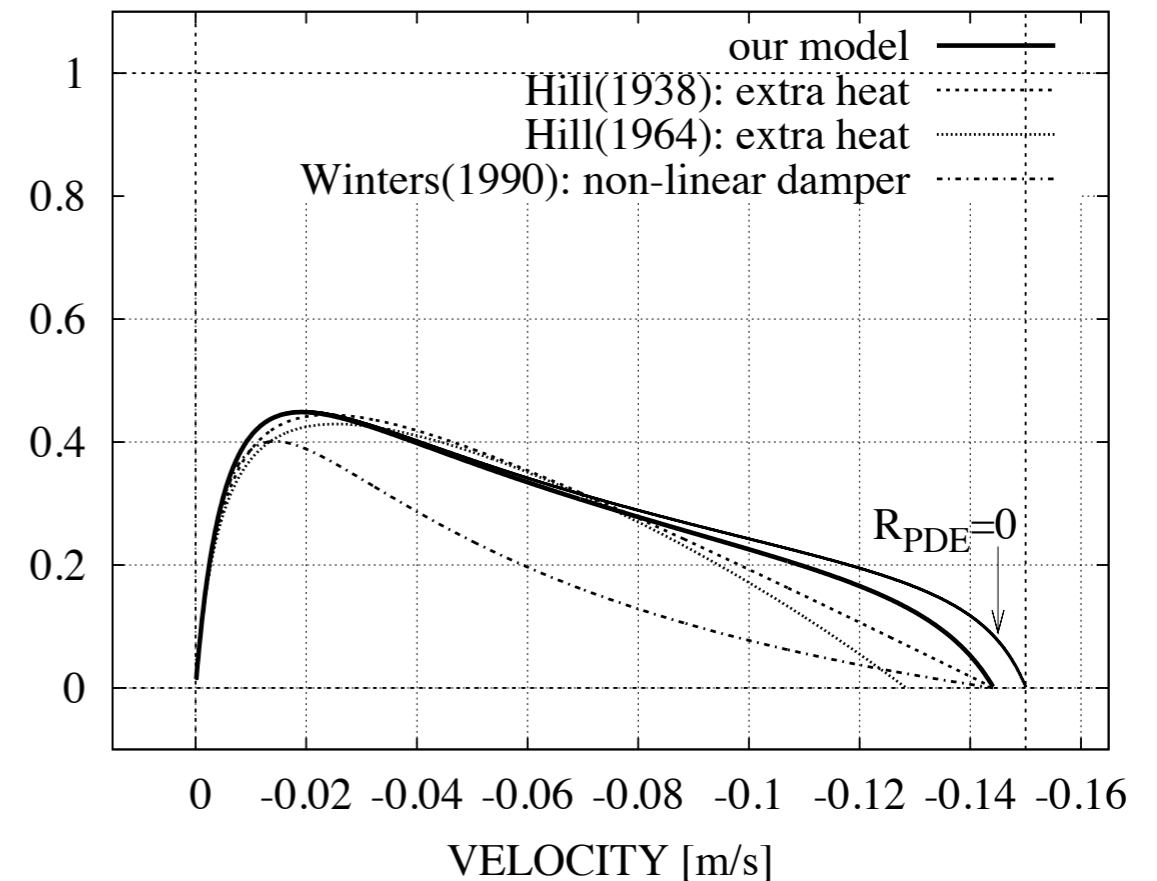
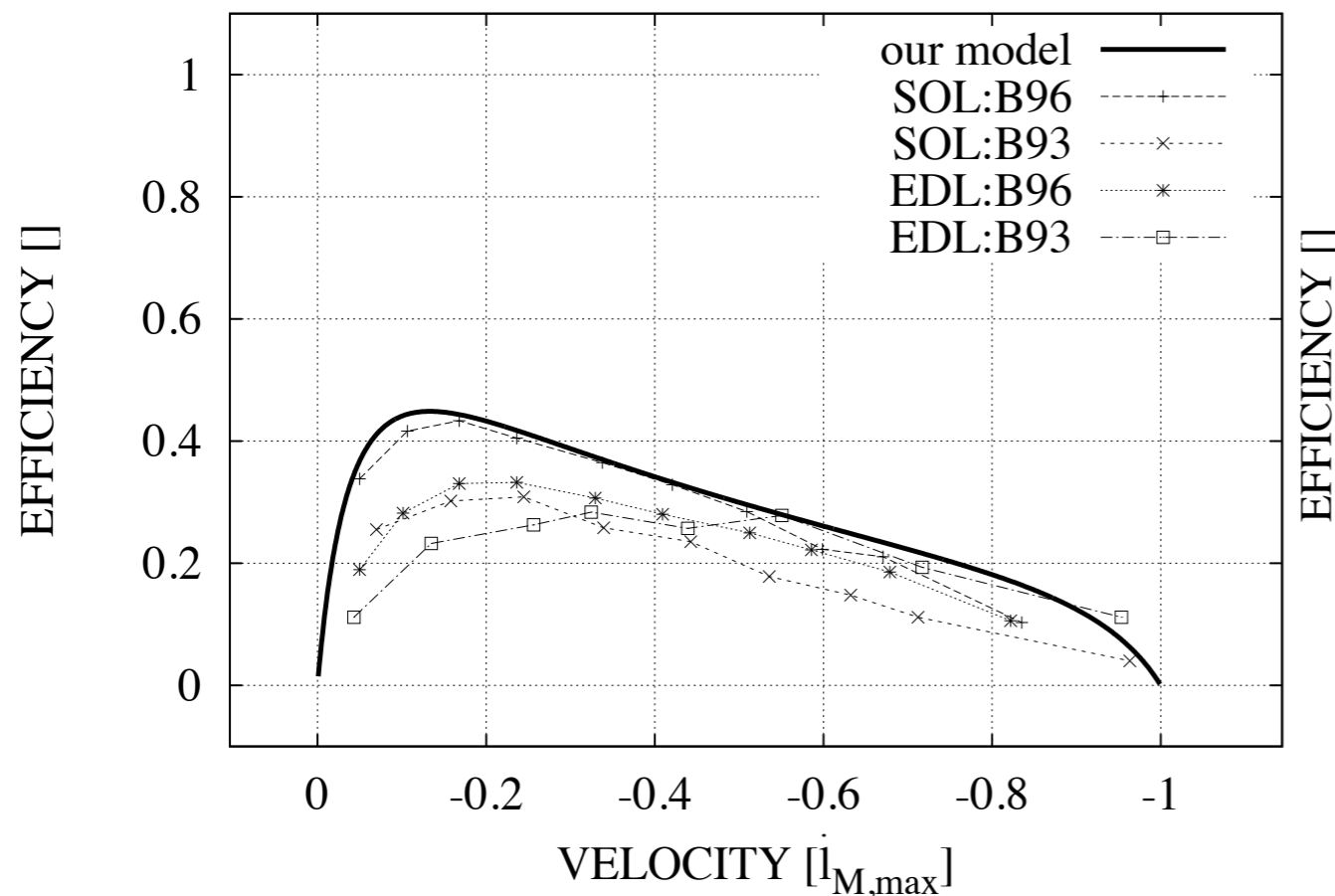
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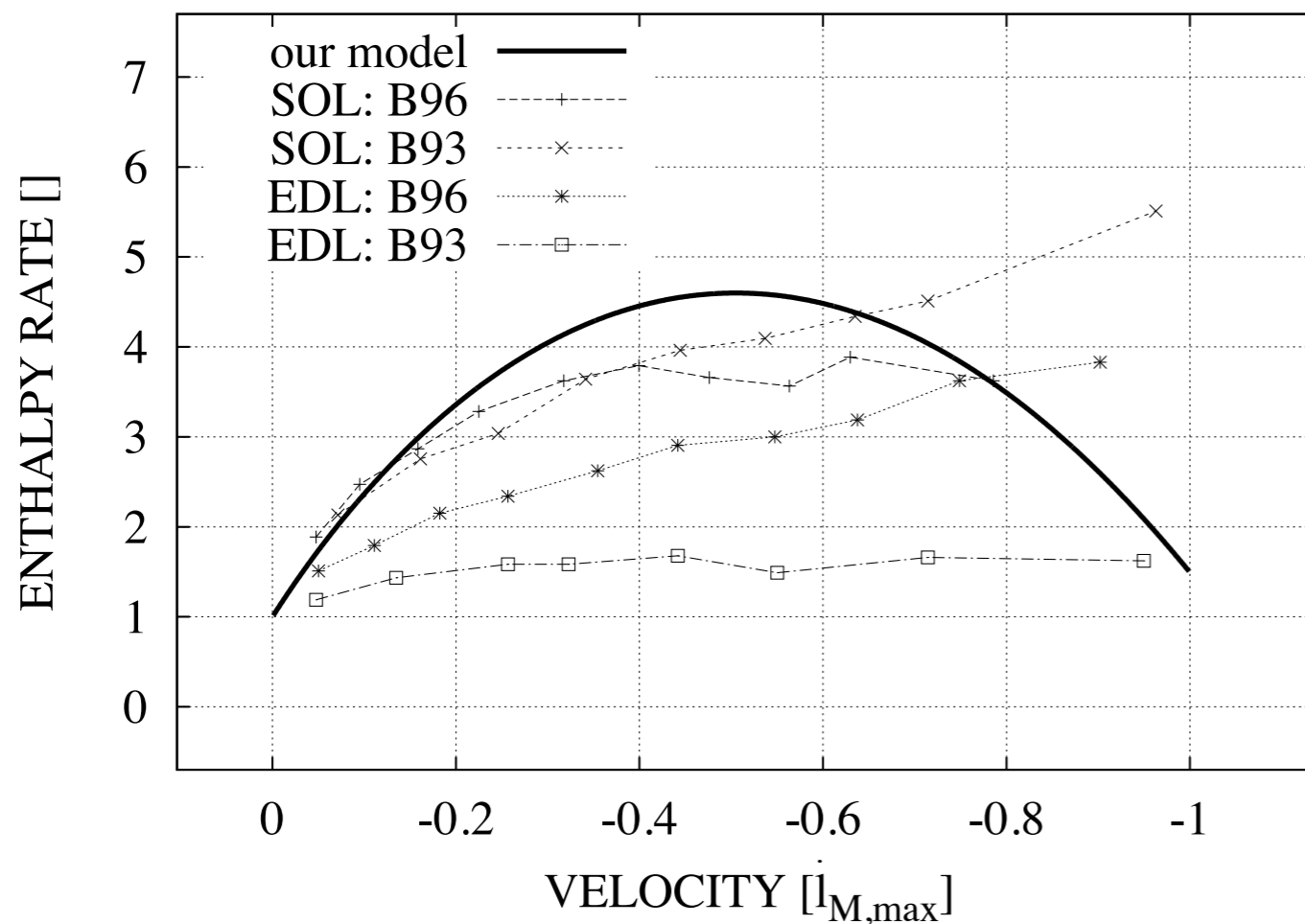
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# Skeletal muscle's mechanics



Efficiency = mech. energy output / mech. energy input

# Skeletal muscle's thermodynamics



Enthalpy rate = power output \* main. heat rate \*  
shortening heat rate



# The biological skeletal muscle's ...

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design and functioning.



# The biological skeletal muscle's ...

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design and functioning.

DESIGN  
CONCEPT?

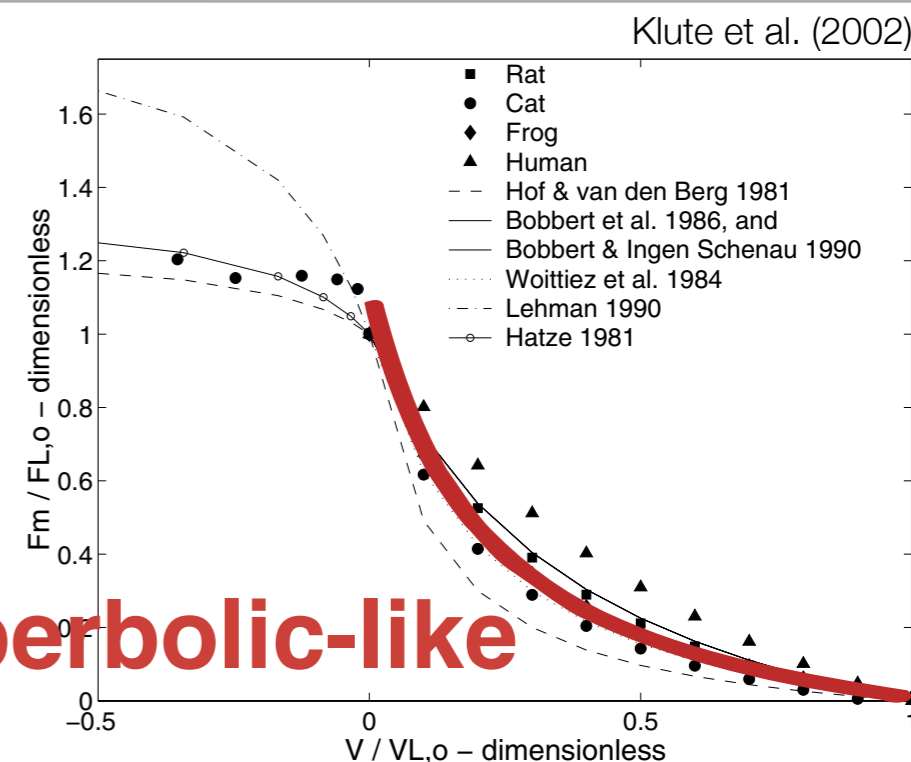
# Design - from biological to artificial muscle ?



Engineering



Biology



Hill-type muscle models so far ...

explain  
predict

+

account for  
structure

# A macroscopic ansatz to derive the Hill relation



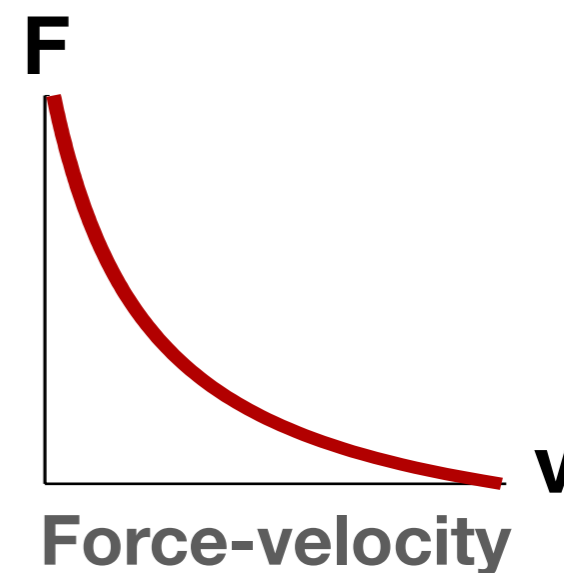
data

classical Hill-type models

CE



fit



# A macroscopic ansatz to derive the Hill relation

classical Hill-type models

data

CE

fit

**F**

**v**

Force-velocity

inspiration

prediction

PDE

SE

AE

assumptions first principle: force equilibrium

force law for damper

define introduced dof

# Analytical model

## A1: Structure + first principle:

$$F_M = F_{SE} = F_{AE} + F_{PDE}$$

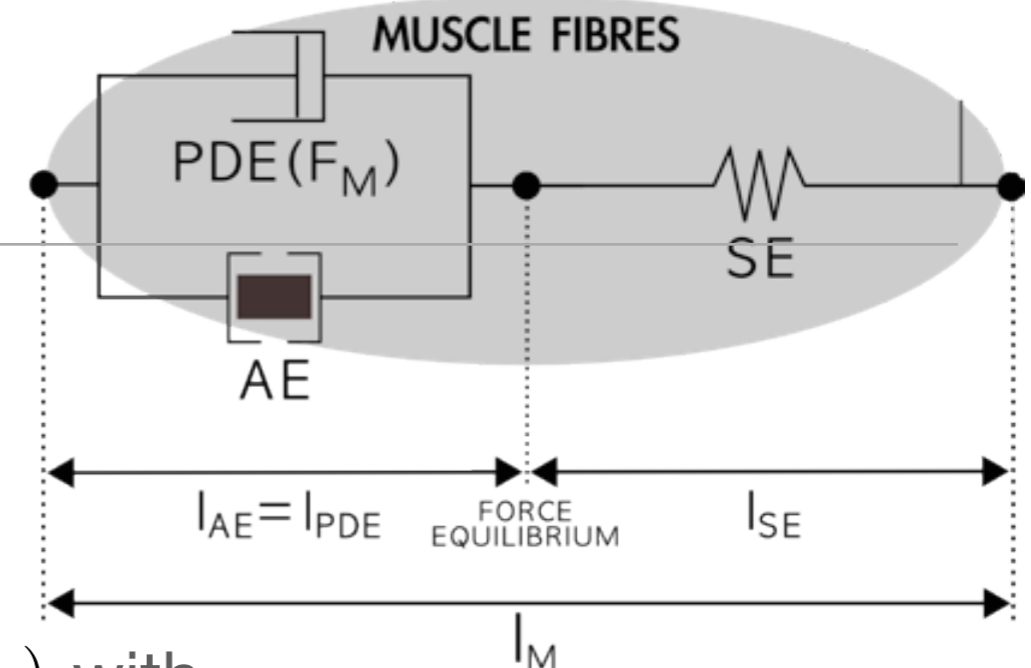
## A2: Choice of a simple force law:

$$F_{PDE} = d_{PDE} \cdot \dot{l}_{PDE} = d_{PDE}(F_M) \cdot (\dot{l}_M - \dot{l}_{SE}) \text{ with}$$

$$d_{PDE}(F_M) = D_{PDE,max} \cdot ((1 - R_{PDE})F_M / F_{AE,max} + R_{PDE})$$

## A3: Internal degree of freedom:

$$\kappa_v = \dot{l}_{SE} / \dot{l}_M$$



# Analytical model

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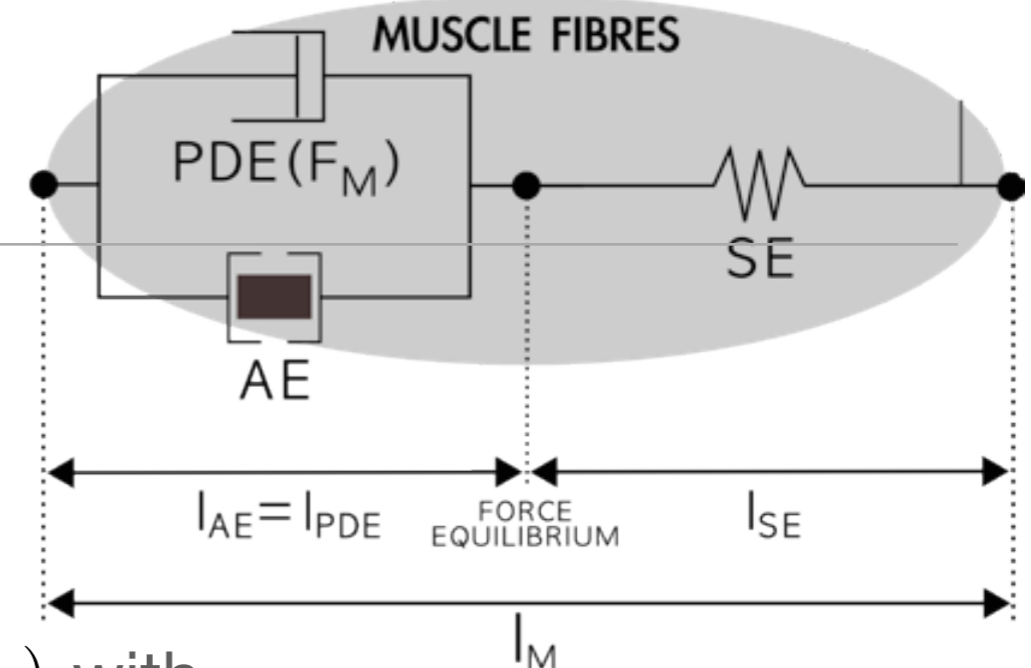
After some mathematics we get:

$$(F_M + A) \cdot \dot{l}_M = -B \cdot (F_{M,0} - F_M)$$

with

$$A = \frac{R_{PDE}}{1 - R_{PDE}} \cdot F_{AE,max}$$

$$B = \frac{1}{1 - R_{PDE}} \cdot \frac{1}{1 - \kappa_v} \cdot \frac{F_{AE,max}}{D_{PDE,max}}$$



# Analytical model

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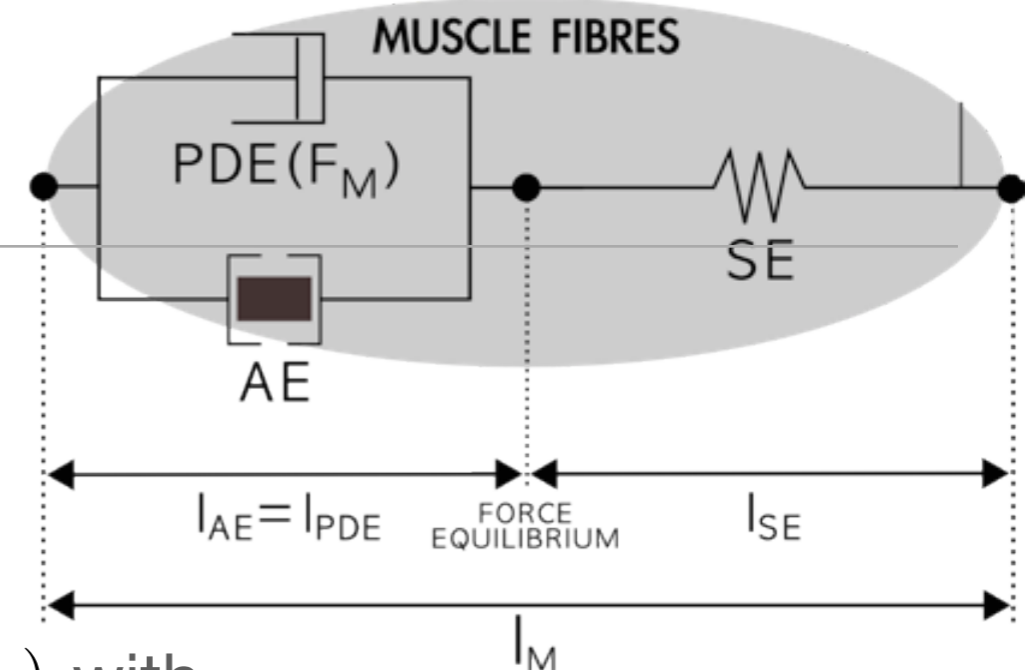
**Hill's original formulation**  
to fit his experimental results

$$(P + a) \cdot v = b \cdot (P_0 - P)$$

with

$$A = \frac{R_{PDE}}{1 - R_{PDE}} \cdot F_{AE,max}$$

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# Analytical model

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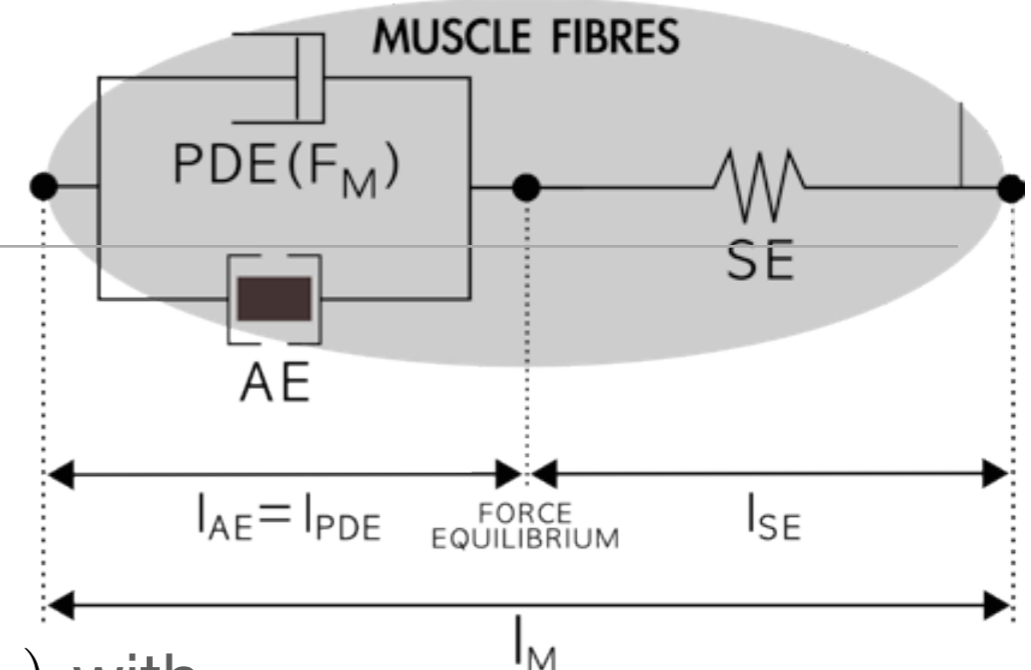
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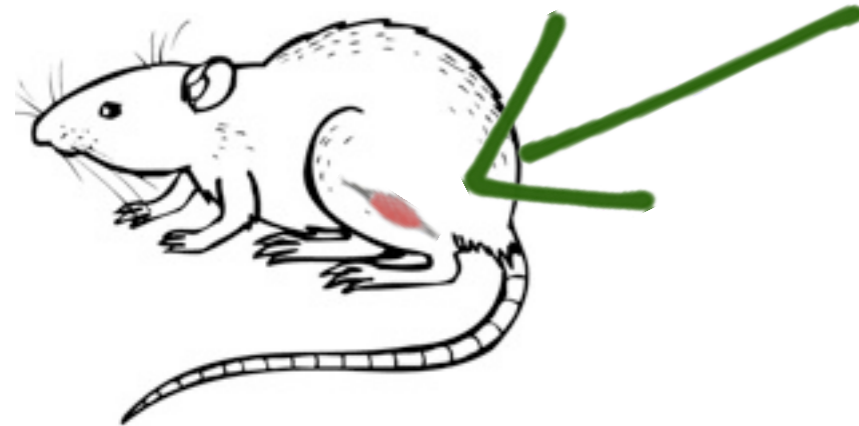
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$$(P + a) \cdot v = b \cdot (F_{max} - P)$$

# Choice of biological muscle (experimental data)



## Rat gastrocnemius

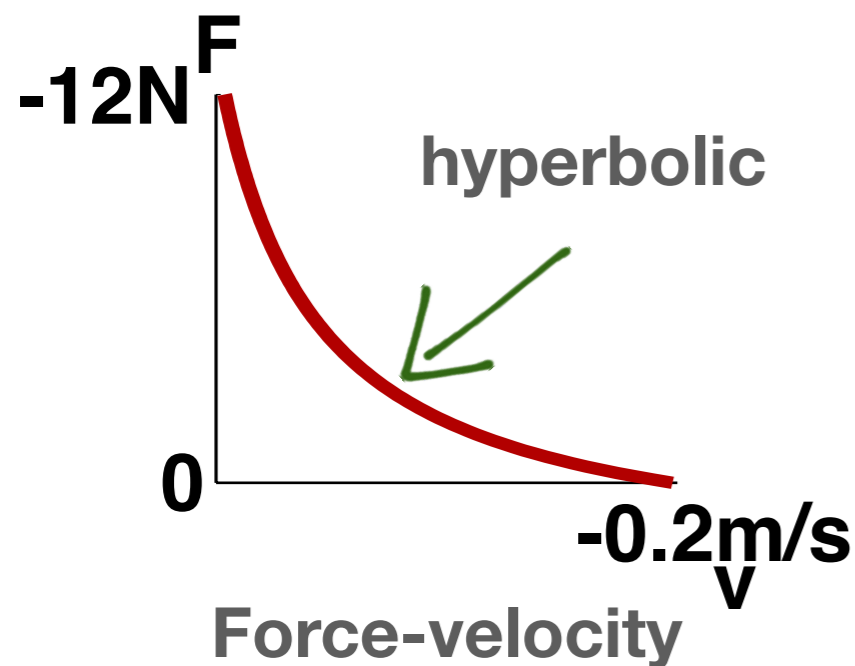
$$A = 2.68 \text{ N}$$

$$B = 0.042 \text{ m/s}$$

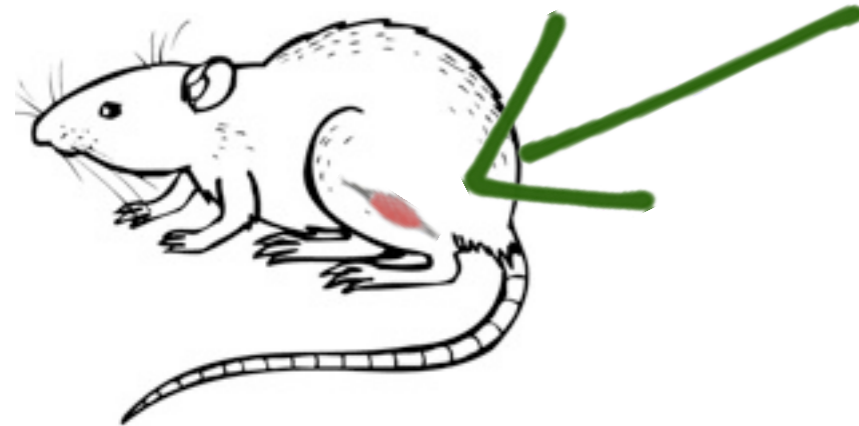
$$F_{\max} = 13.4 \text{ N}$$

$$l_{CE,opt} = 0.013 \text{ m}$$

van Zandwijk et al. 1996



# Choice of biological muscle (experimental data)



## Rat gastrocnemius

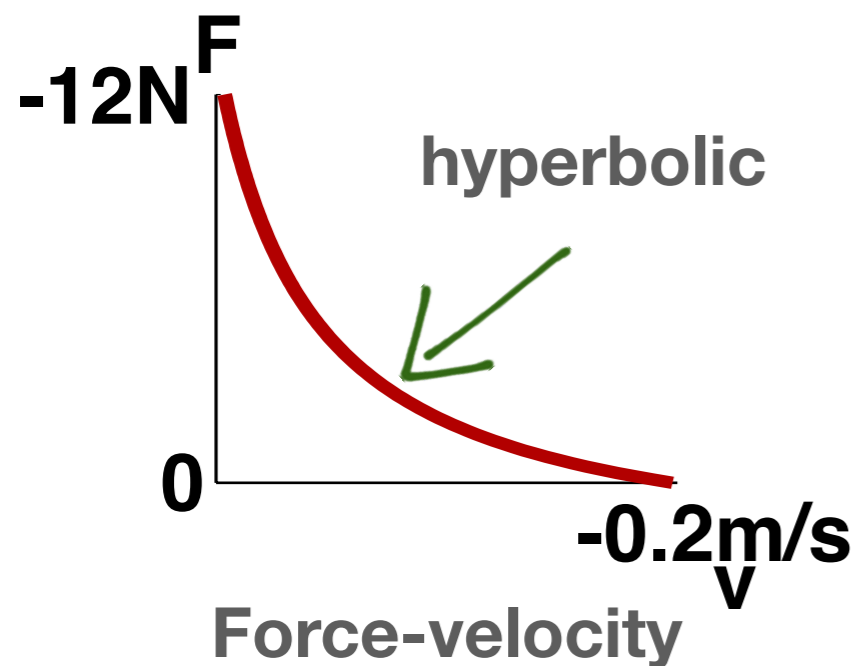
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$$F_{\max} = 13.4 \text{ N}$$

$$l_{CE,opt} = 0.013 \text{ m}$$

van Zandwijk et al. 1996



analytical model

$$\kappa_v = 0.15$$

$$F_{AE,max} = F_{\max}$$

$$F_{M,0} = F_{AE,max}$$

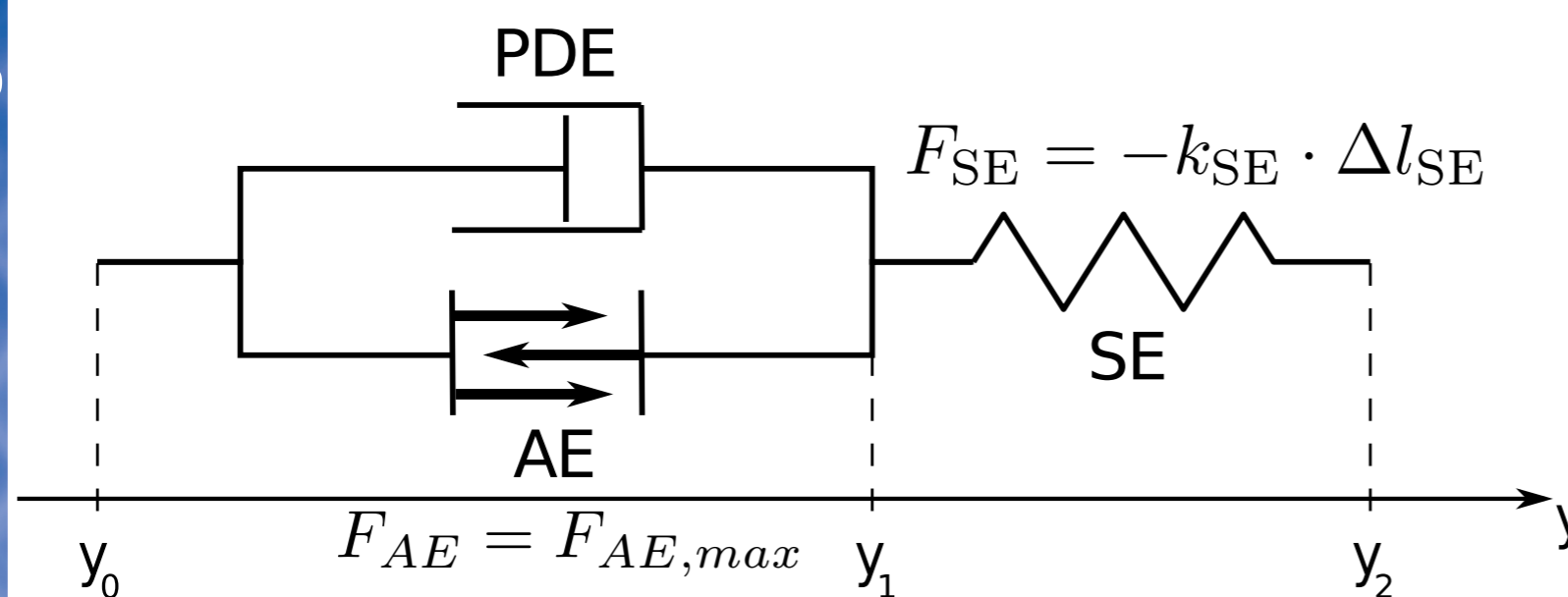
analytical model

## Mechanical parameters PDE

$$R_{PDE} = 0.2$$

$$D_{PDE,max} = 386 \text{ Ns/m}$$

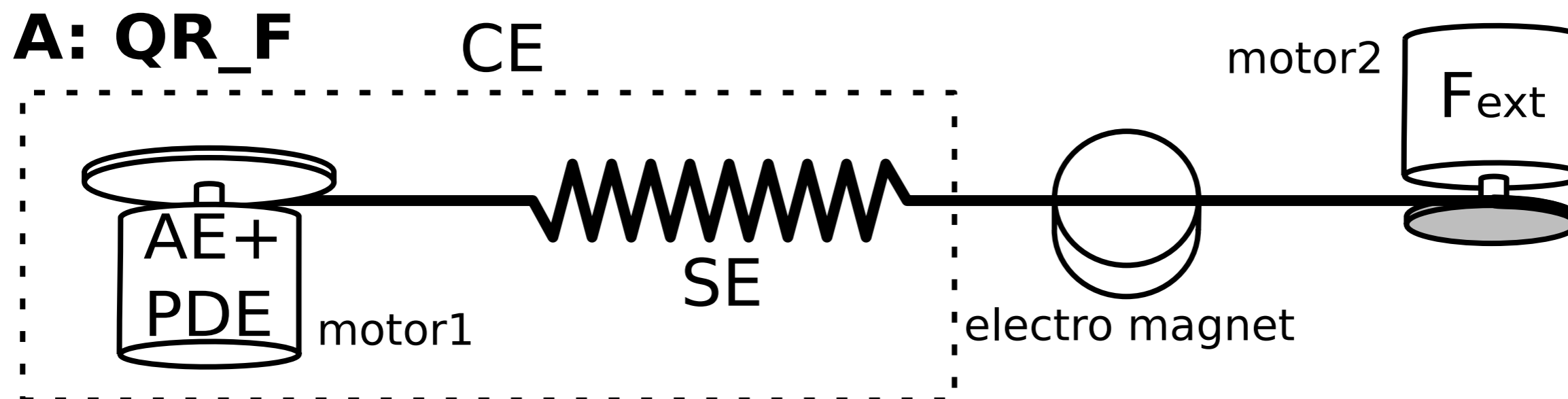
# Numerical model and hardware experiment



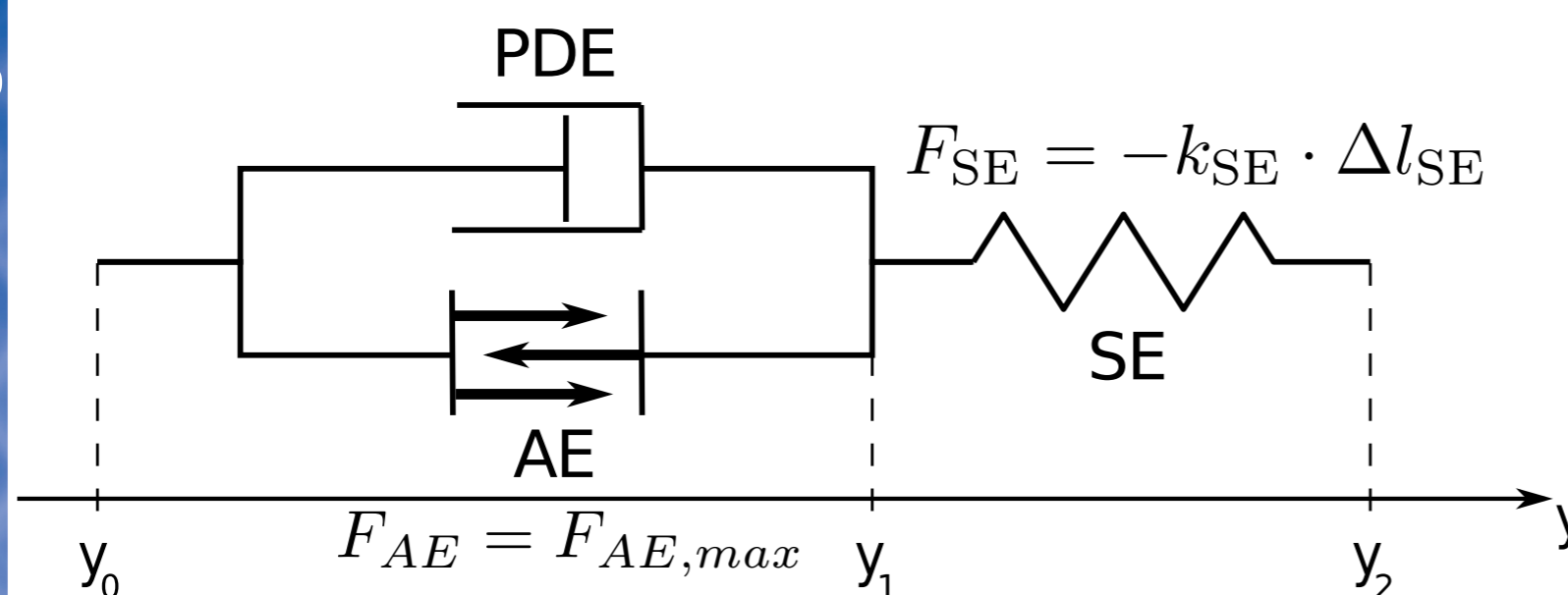
$$\dot{y}_1 = \frac{F_{AE} - F_{SE}}{d_{PDE}(F_M)}$$

$$\ddot{y}_2 = g + \frac{1}{m} F_{SE}$$

**using same  
parameters**



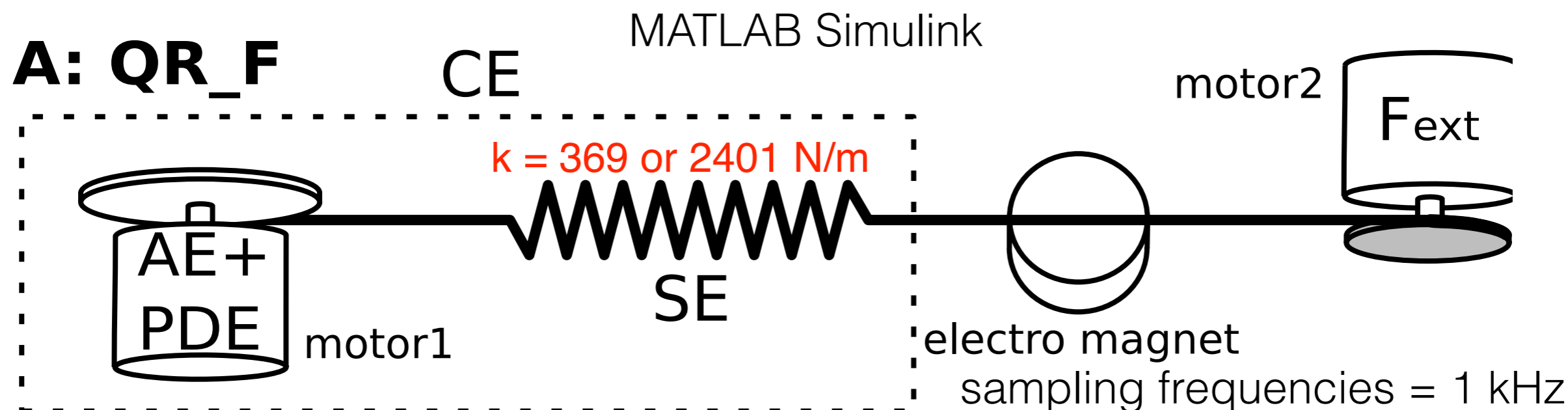
# Numerical model and hardware experiment



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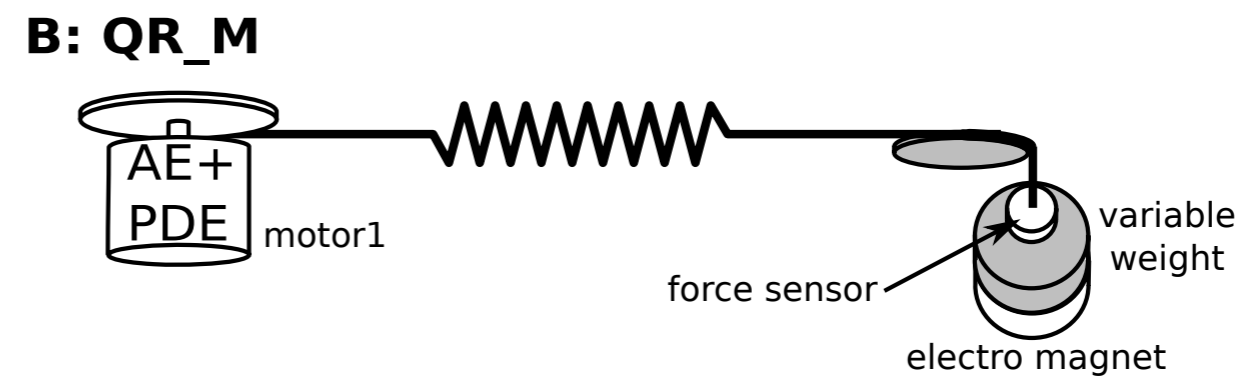
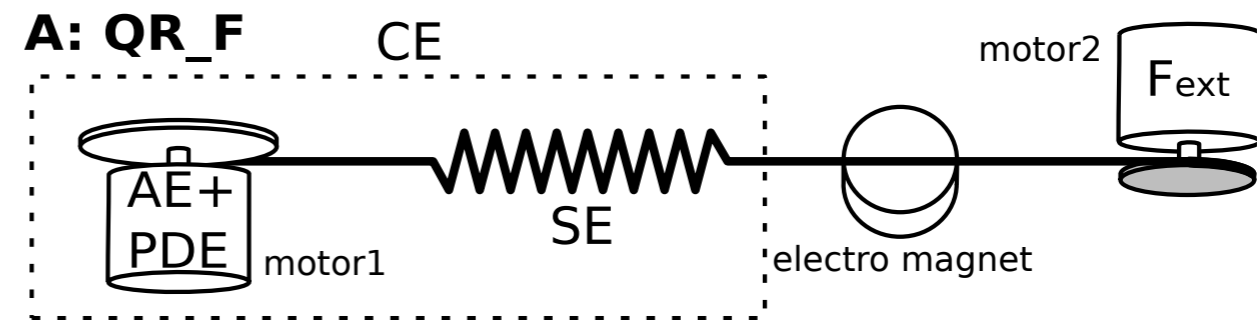
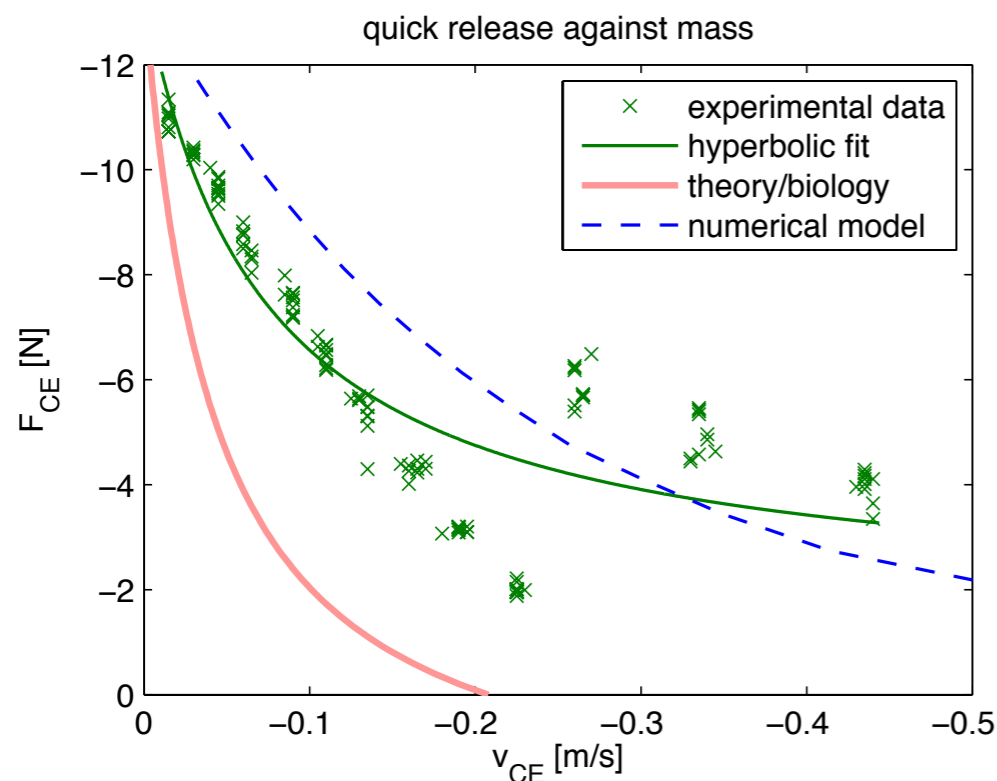
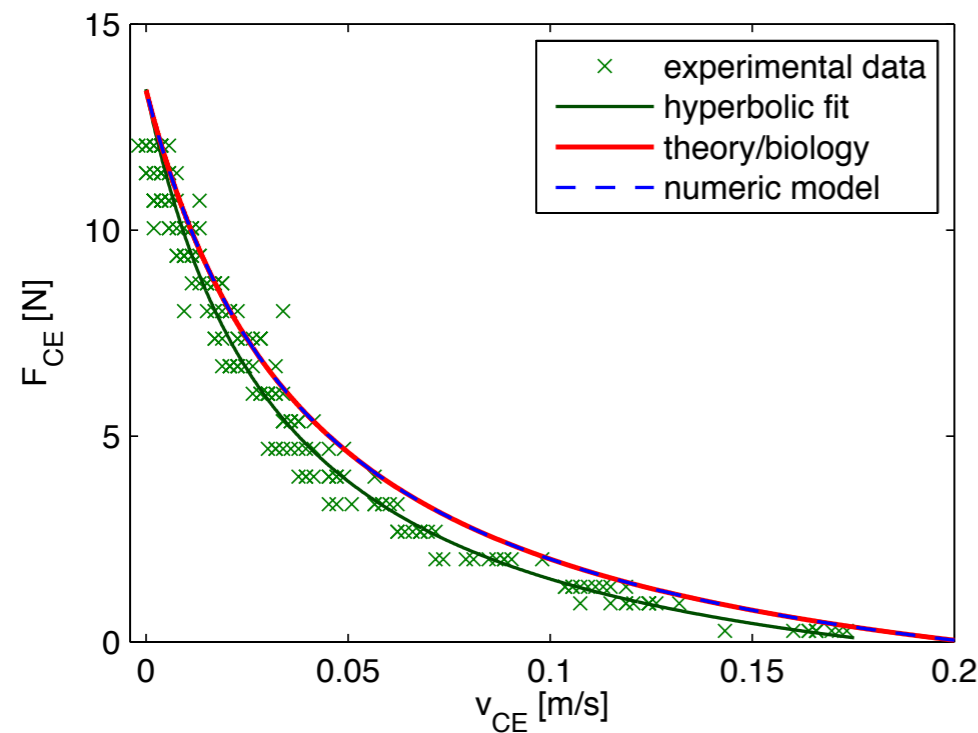
$$\ddot{y}_2 = g + \frac{1}{m} F_{SE}$$

**using same  
parameters**



**Quick release contractions**

# Hyperbolic force velocity relation



Haeufle, D.F.B., Günther, M., Blickhan, R., Schmitt, S. (2012). Can Quick Release Experiments Reveal the Muscle Structure? A Bionic Approach. Journal of Bionic Engineering, 9(2), 211-223

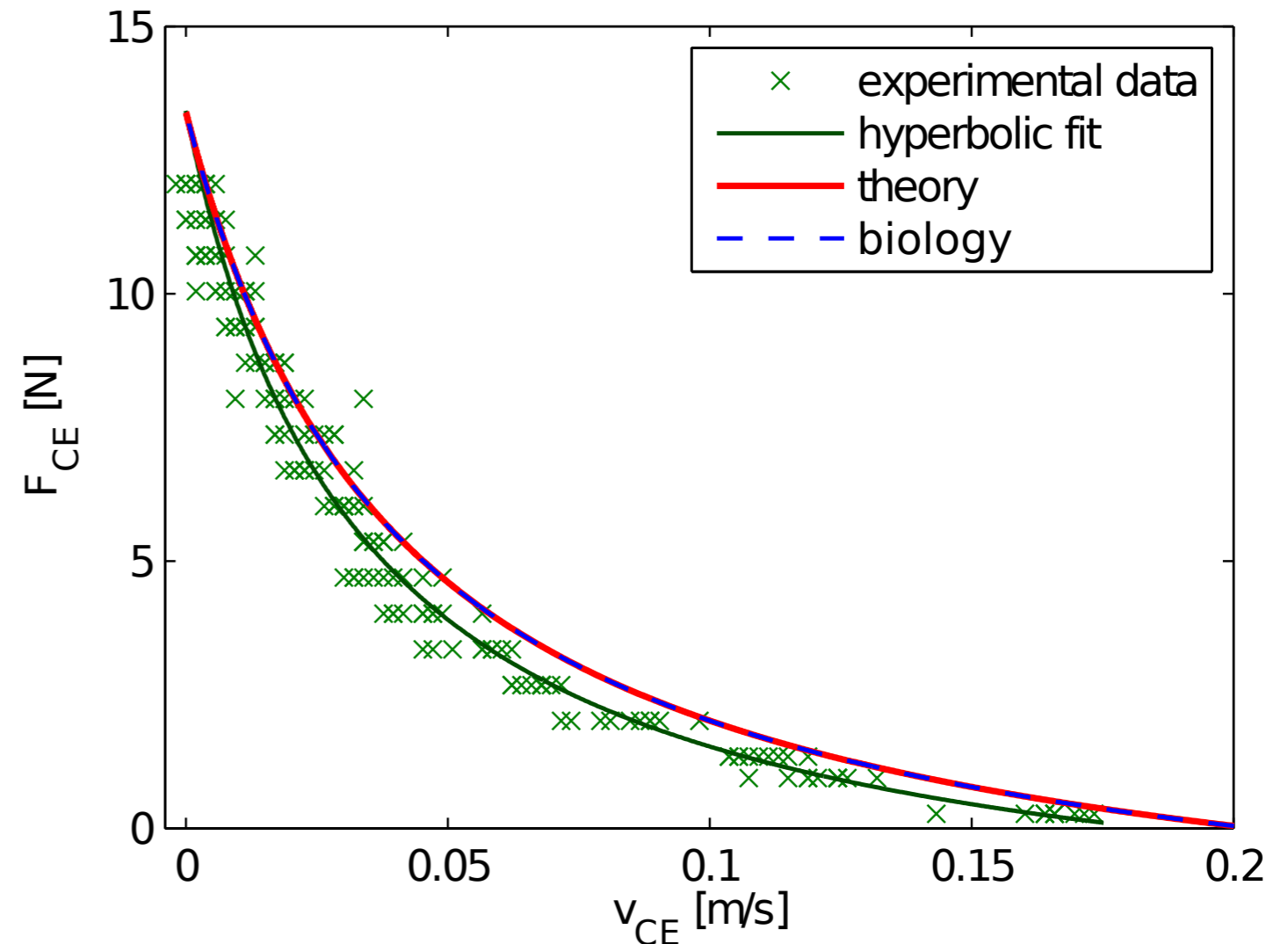
# Biological muscle is the better actuator!



Engineering



Biology



Schmitt, S., Häufle, D.F.B., Blickhan, R., Günther, M. (2012). Nature as an engineer: one simple concept of a bio-inspired functional artificial muscle. *Bioinspiration & Biomimetics*, 7 036022

Haeufle, D.F.B., Günther, M., Blickhan, R., Schmitt, S. (2012). Can Quick Release Experiments Reveal the Muscle Structure? A Bionic Approach. *Journal of Bionic Engineering*, 9(2), 211-223

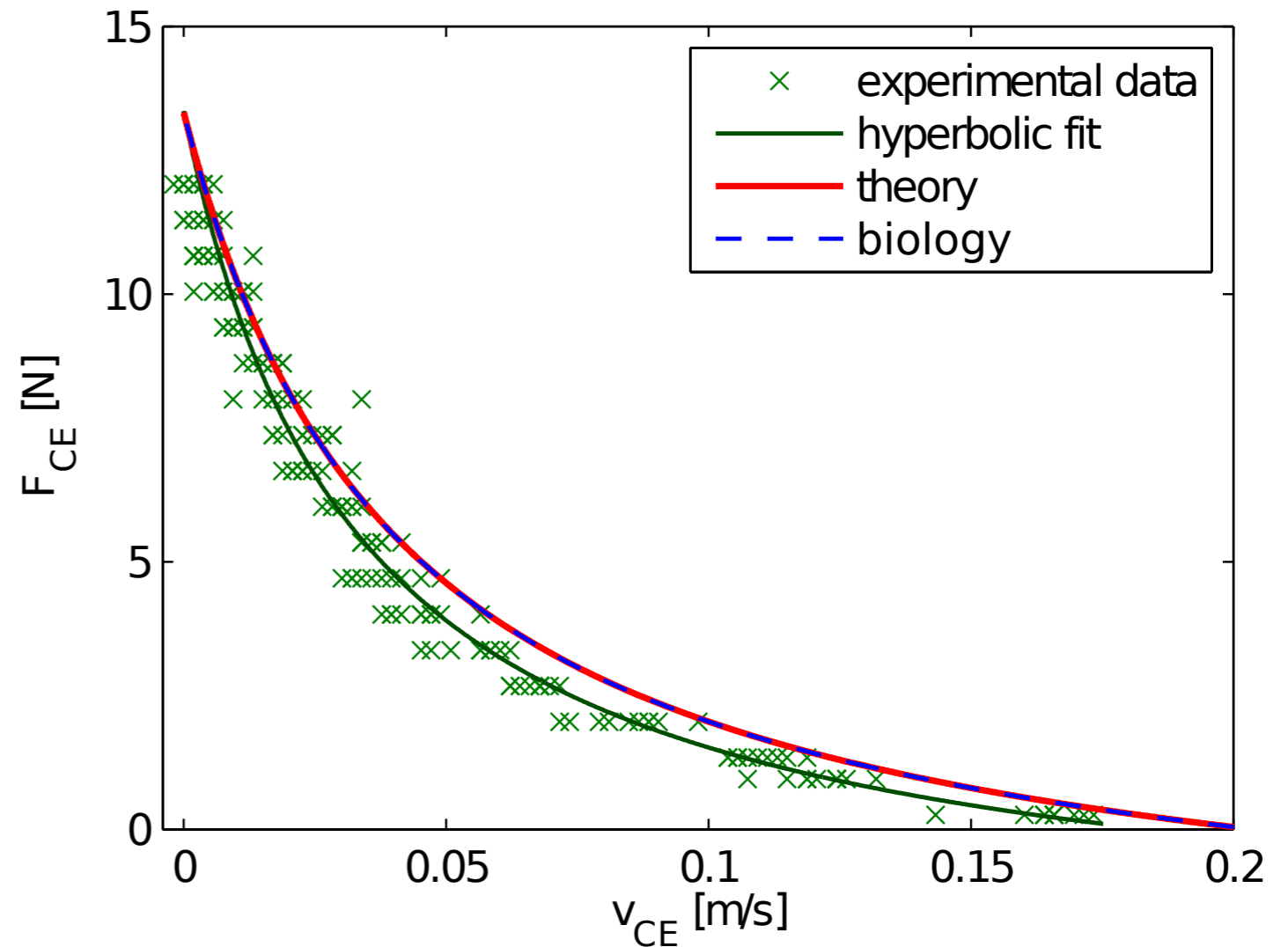
# Biological muscle is the better actuator!



Engineering



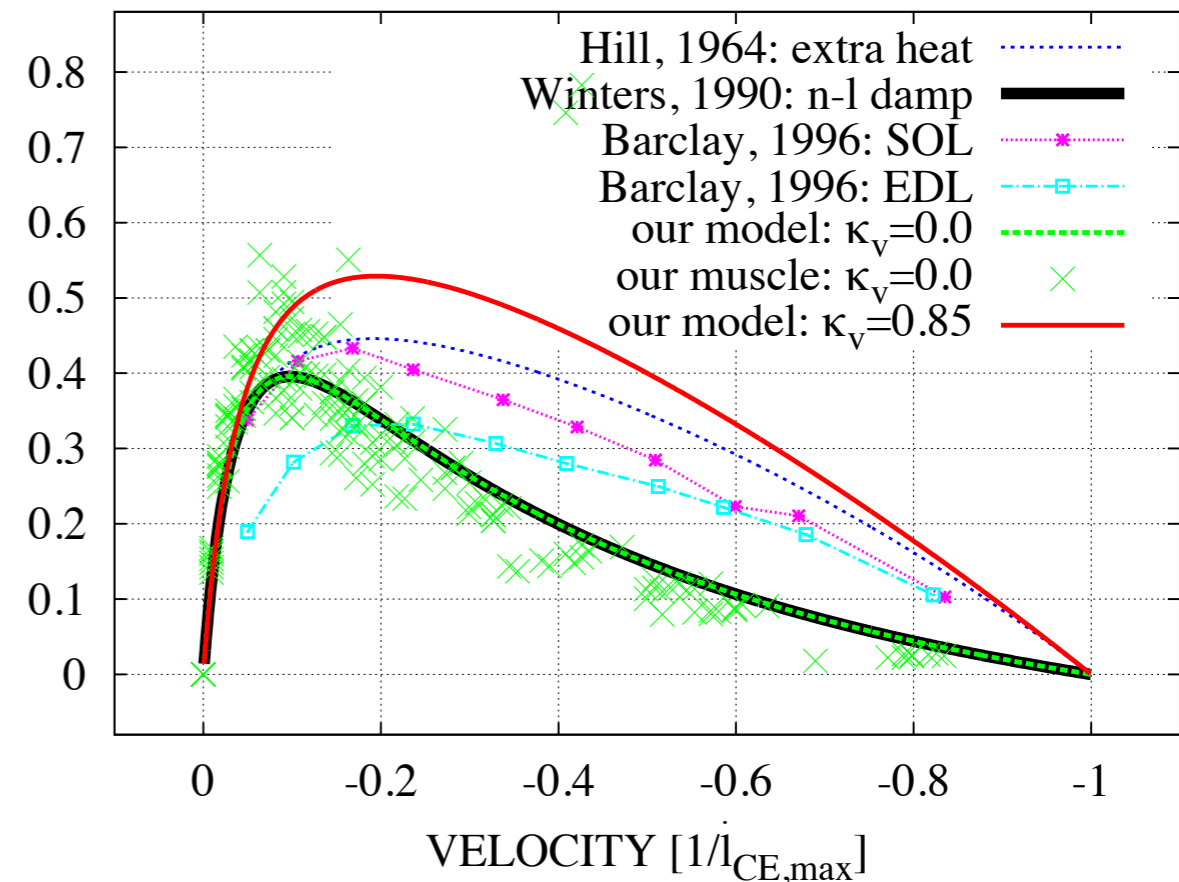
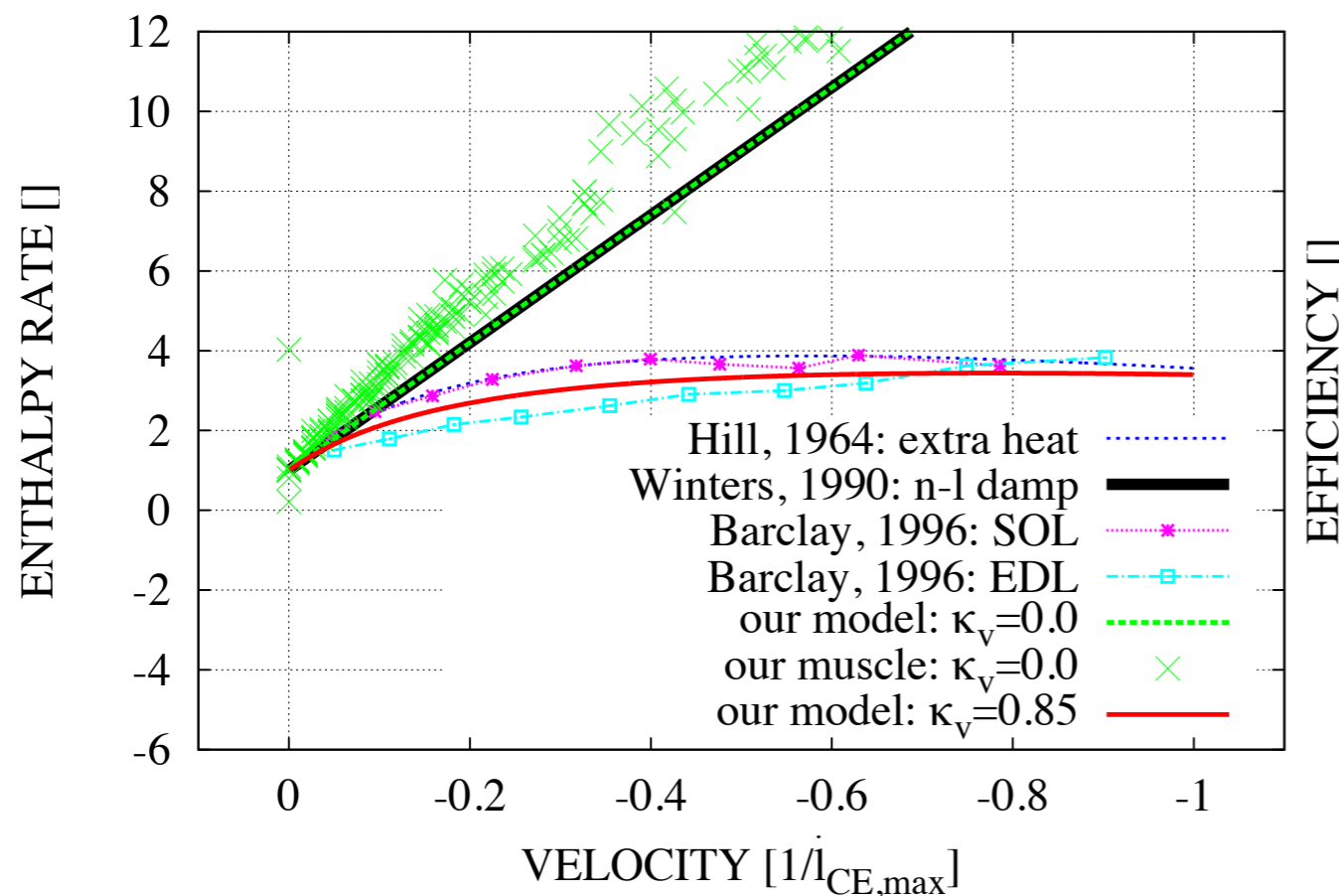
Biology



Schmitt, S., Häufle, D.F.B., Blickhan, R., Günther, M. (2012). Nature as an engineer: one simple concept of a bio-inspired functional artificial muscle. *Bioinspiration & Biomimetics*, 7 036022

Haeufle, D.F.B., Günther, M., Blickhan, R., Schmitt, S. (2012). Can Quick Release Experiments Reveal the Muscle Structure? A Bionic Approach. *Journal of Bionic Engineering*, 9(2), 211-223

# Is biological muscle the better actuator?



Enthalpy rate = energy balance including heat rates



# What to do with this knowledge?

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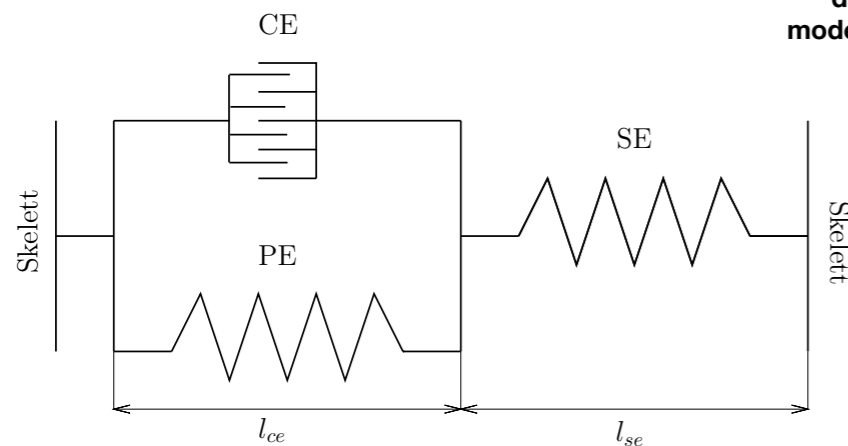
Build computer models of the biological system, which then can be activated and validated, realistically!

# Our view on the biological motor ...

## Muscle

Hill-type muscle model:

Günther, Schmitt, Wank (2007). **High-frequency oscillations as a consequence of neglected serial damping in Hill-type muscle models.** Biological Cybernetics, 97(1), 63-79..



$$v_j^{CE} = f_v(l_j^{mtc}, l_j^{CE}, q_j)$$

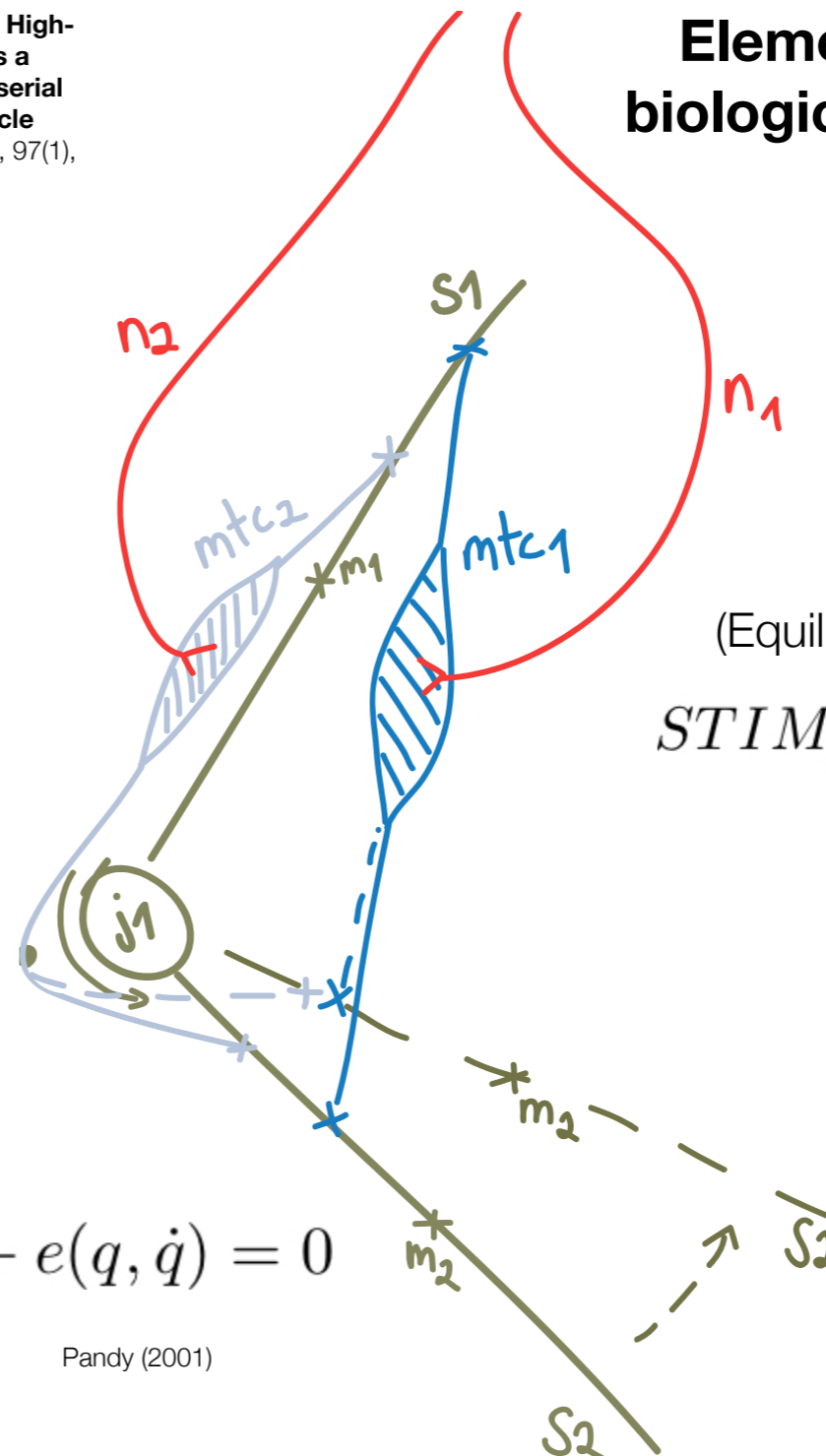
$$f_j^{mtc} = f_f(l_j^{CE}, v_j^{CE}, q_j)$$

$$\dot{q}_j = f_{qd}(l_j^{mtc}, l_j^{CE}, STIM_j^i)$$

## Skeletal apparatus

Model of the mechanical system:

$$M(q)\ddot{q} + C(q)\dot{q}^2 + g(q) + R(q)f^{mtc} + e(q, \dot{q}) = 0$$



## Elementary biological drive

## Motor control

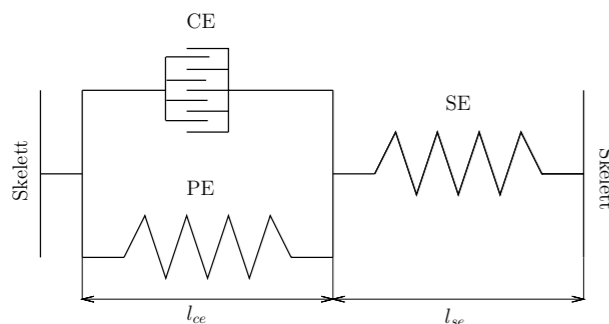
(Equilibrium-Point-Theory, EPT):

$$STIM_j^i = f_s(\lambda_j^i, l_j^{CE}, v_j^{CE})$$

# Modelling and simulation - our approach

## Muscle

Hill-type muscle model:



$$v_j^{CE} = f_v(l_j^{mtc}, l_j^{CE}, q_j)$$

$$f_j^{mtc} = f_f(l_j^{CE}, v_j^{CE}, q_j)$$

$$\dot{q}_j = f_{qd}(l_j^{mtc}, l_j^{CE}, STIM_j^i)$$

## Skeletal apparatus

Model of the mechanical system:

$$M(q)\ddot{q} + C(q)\dot{q}^2 + g(q) + R(q)f^{mtc} + e(q, \dot{q}) = 0$$

Pandy (2001)

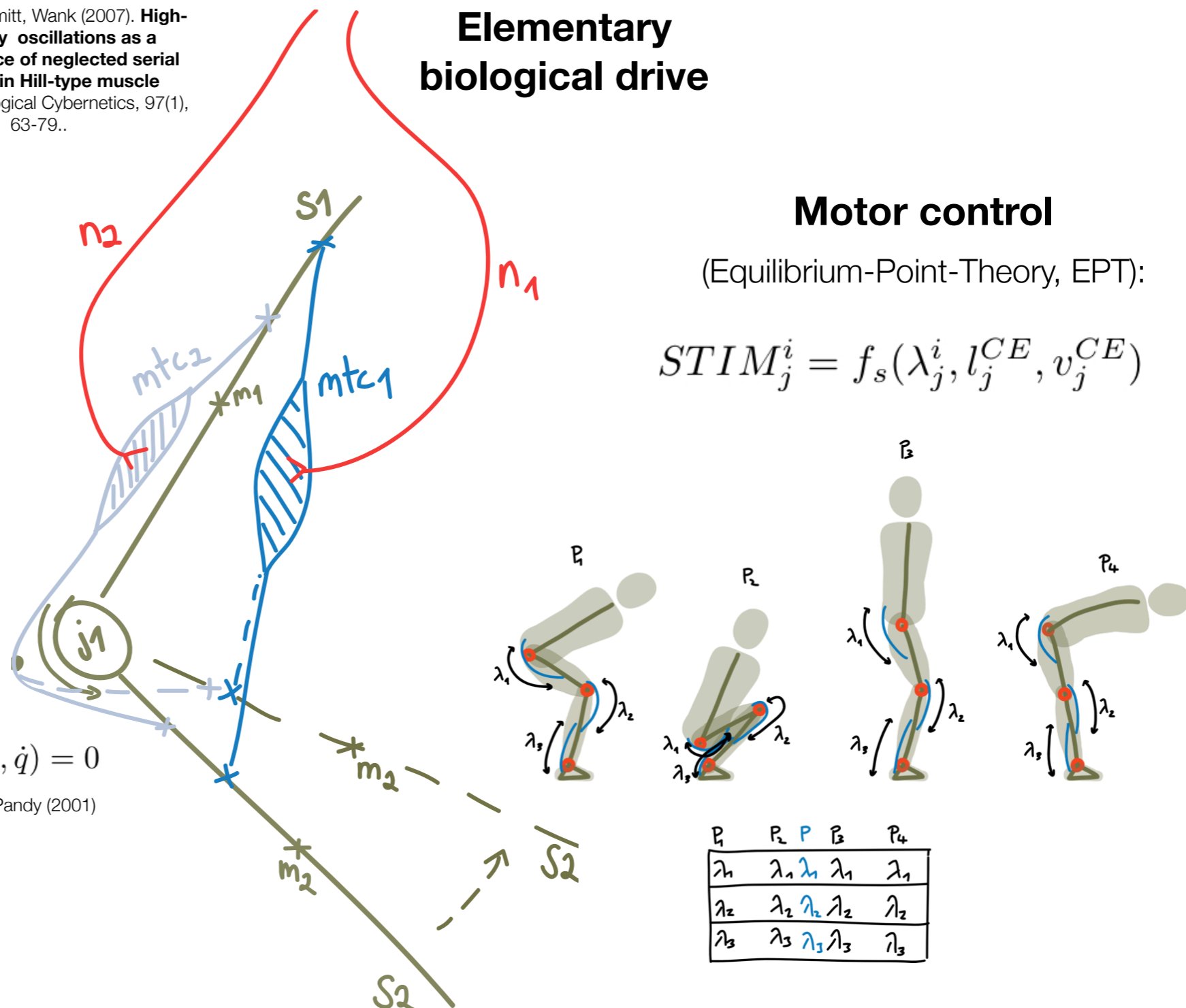
Günther, Schmitt, Wank (2007). **High-frequency oscillations as a consequence of neglected serial damping in Hill-type muscle models.** Biological Cybernetics, 97(1), 63-79..

## Elementary biological drive

## Motor control

(Equilibrium-Point-Theory, EPT):

$$STIM_j^i = f_s(\lambda_j^i, l_j^{CE}, v_j^{CE})$$



# Modelling and simulation - motor control

***multiple EBDs (single joint drives)***

+

***more complex drives  
(multi joint drives)***

+

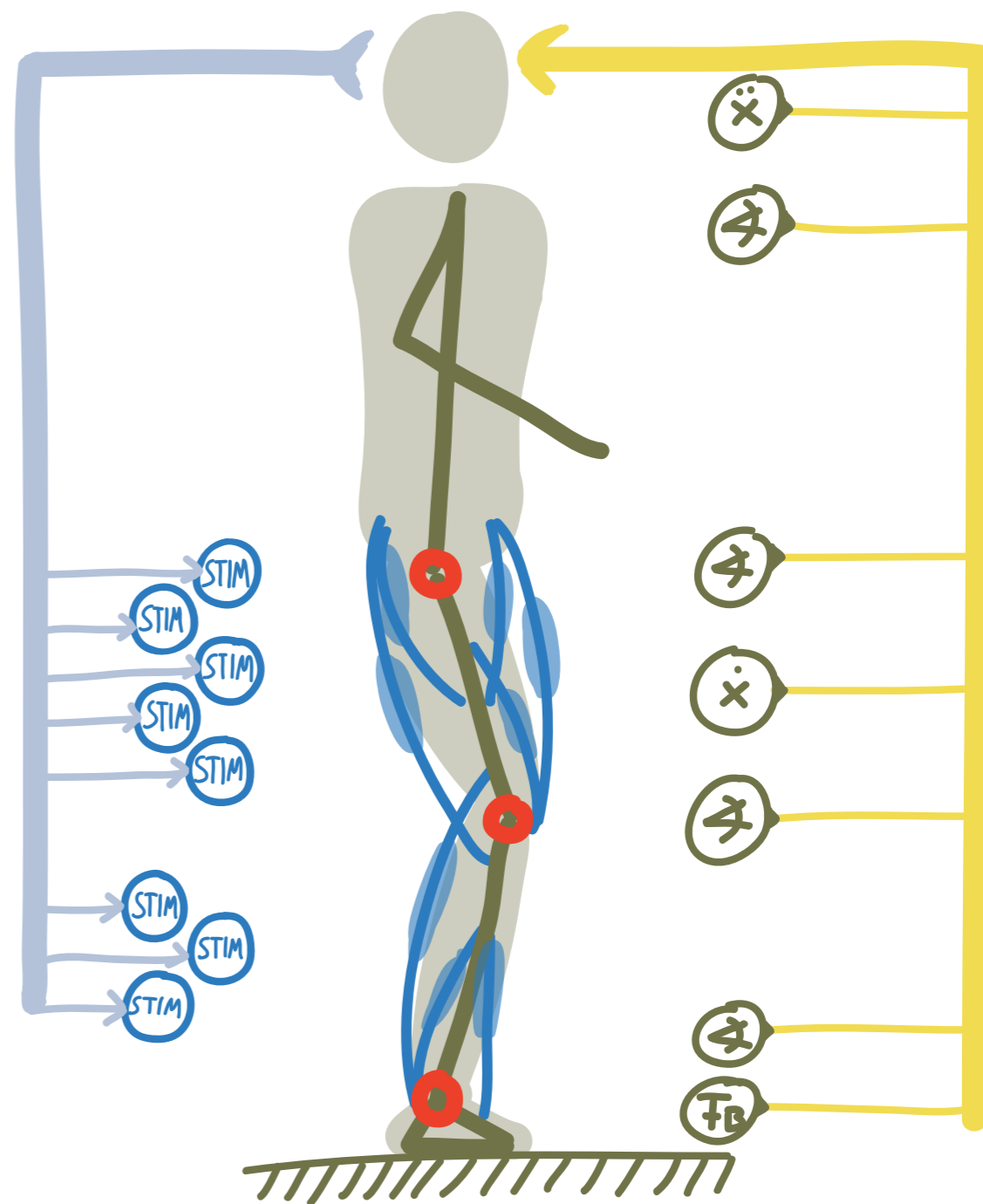
***well tuned control (all drives)***

+

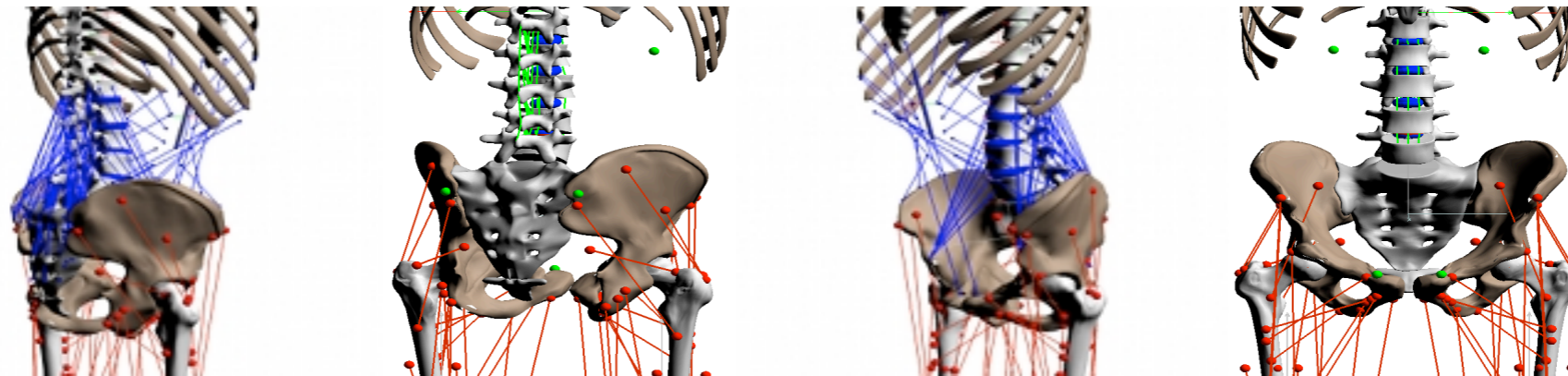
***movement tasks (daily living, ...)***

+

***disturbances (uneven ground,  
impact forces, ...)***



# Modelling and simulation of human lumbar spine



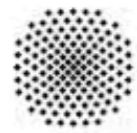
<b>450</b>	degrees of freedom
<b>48</b>	mechanical dofs
<b>202</b>	Muscle-tendon complex (active, Hill-type)
<b>58</b>	non-linear ligaments
<b>5</b>	intervertebral discs (non-linear, coupled)

Anatomy of skeleton: m, 68kg, 1,78m (NASA, 1978)

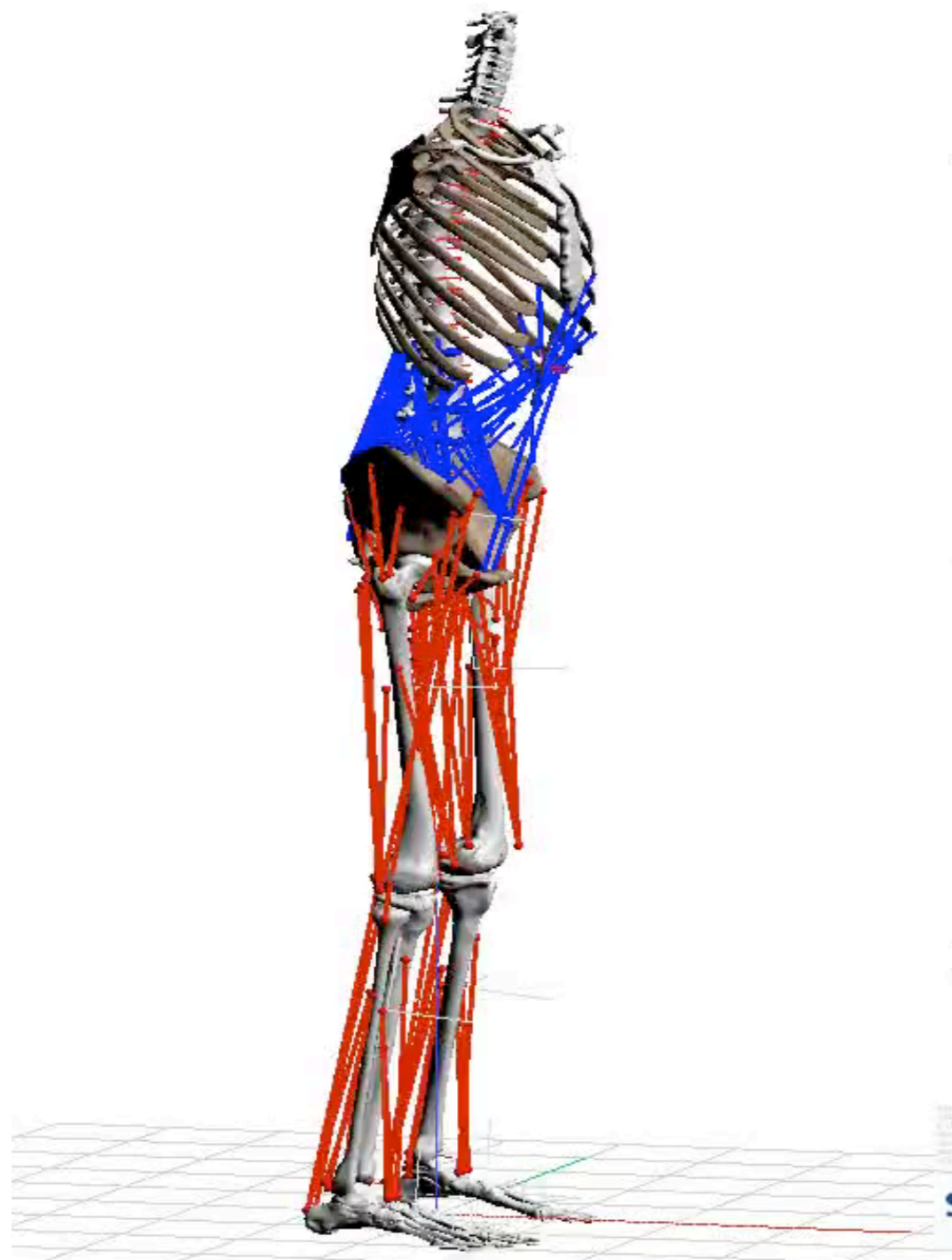
Ligaments: Anatomy (Panjabi, 1982), physiology (Chazal, 1985)

Muscles: Anatomy and physiology (Bogduk, 1992a,b, 1998;  
Hansen, 2006; Christophy, 2012)

# Modelling and simulation of human lumbar spine



University of Stuttgart  
Germany



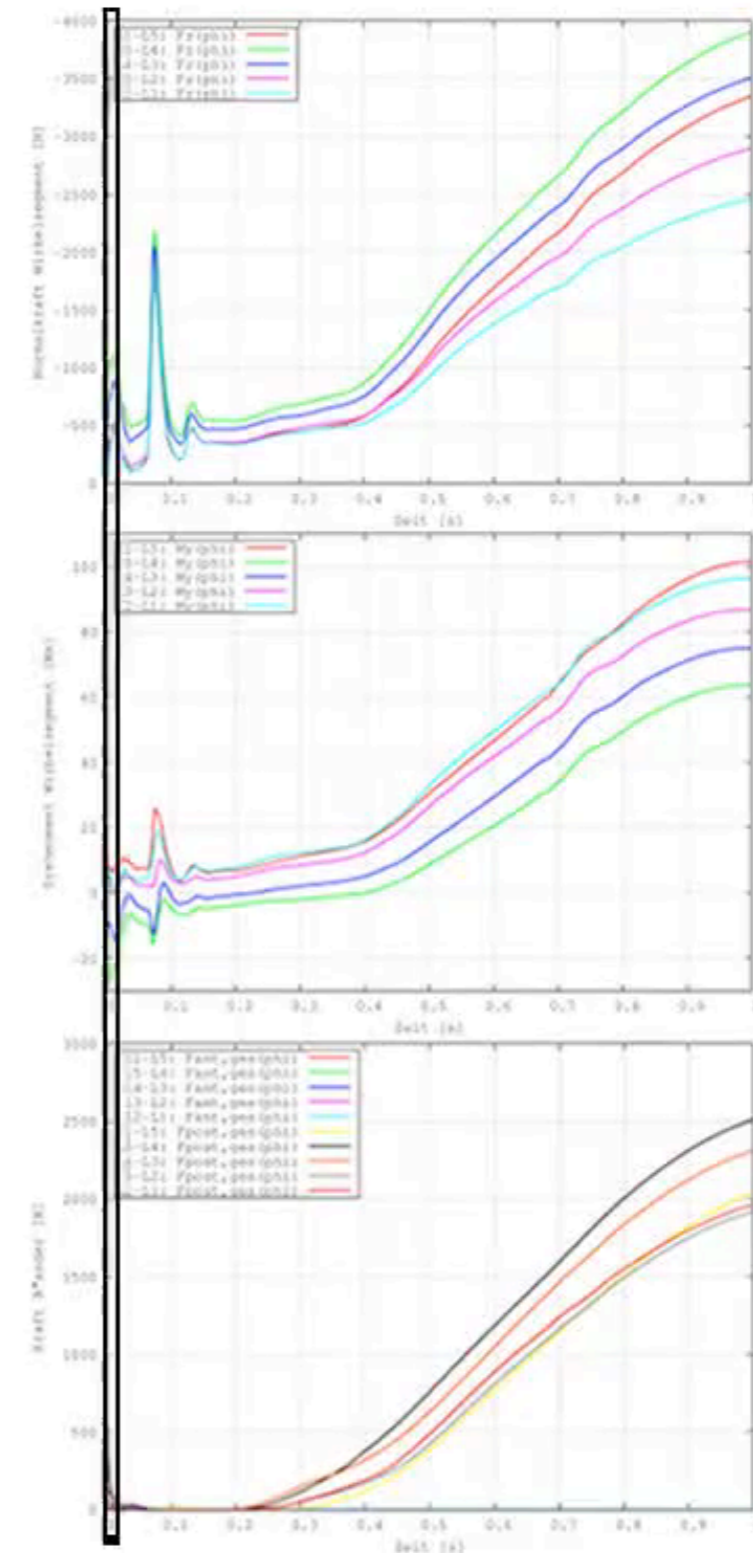
IVD Force  
normal dir.

IVD Torque

LIG Force  
posterior

The Human Movement  
Simulation Lab

SimTech  
Cluster of Excellence



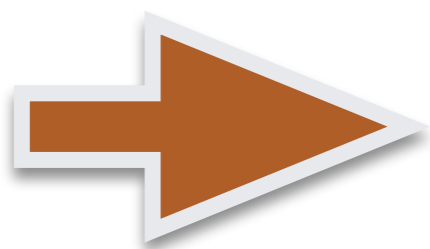


# Motions in Man and Machine

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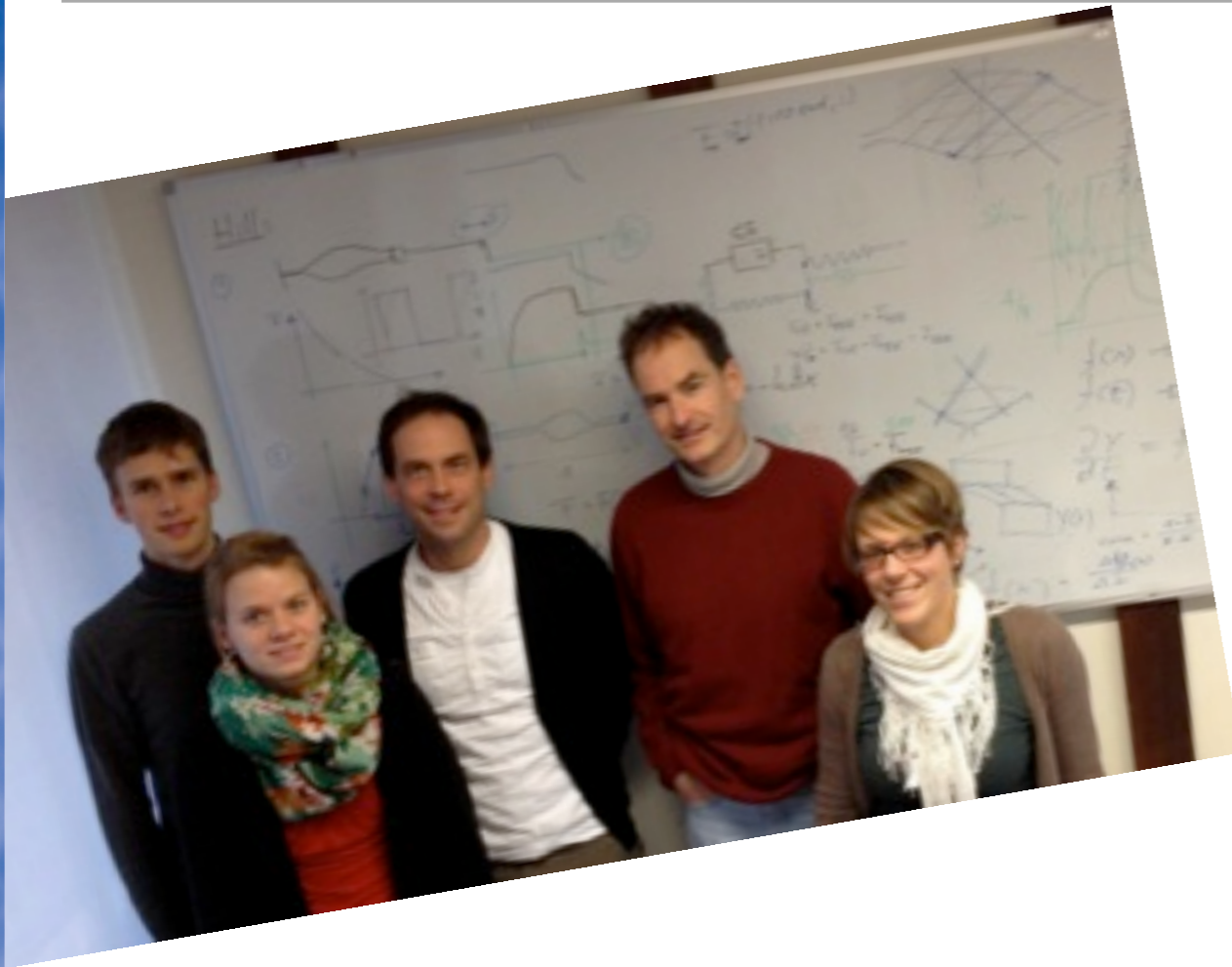
A joint task for two groups:

- (1) Computer simulation of an arm movement
- (2) 3-d movement analysis of an arm movement



Project work will be to do (1) and (2)  
and compare simulation and experiment

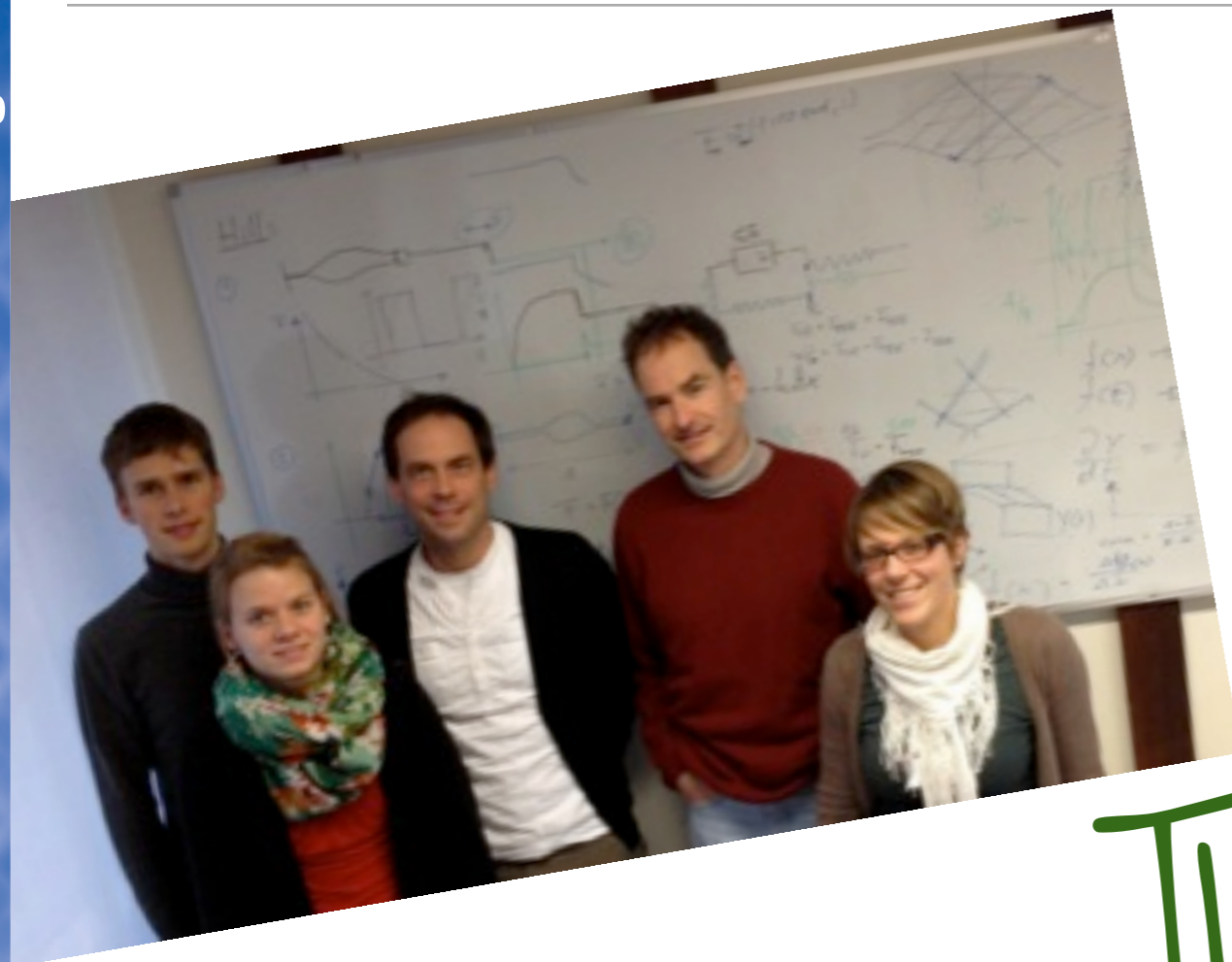
# The **Human Movement Simulation** Lab



**Alexandra Bayer**  
**Michael Günther**  
**Daniel Häufle**  
**Tille Rupp**  
**Syn Schmitt**



# The **Human Movement Simulation** Lab



Alexandra Bayer

Michael Günther

Daniel Häufle

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Thank you for  
your attention !